

Advances and problems in the modeling of powder materials sintering with direct heating by electric current

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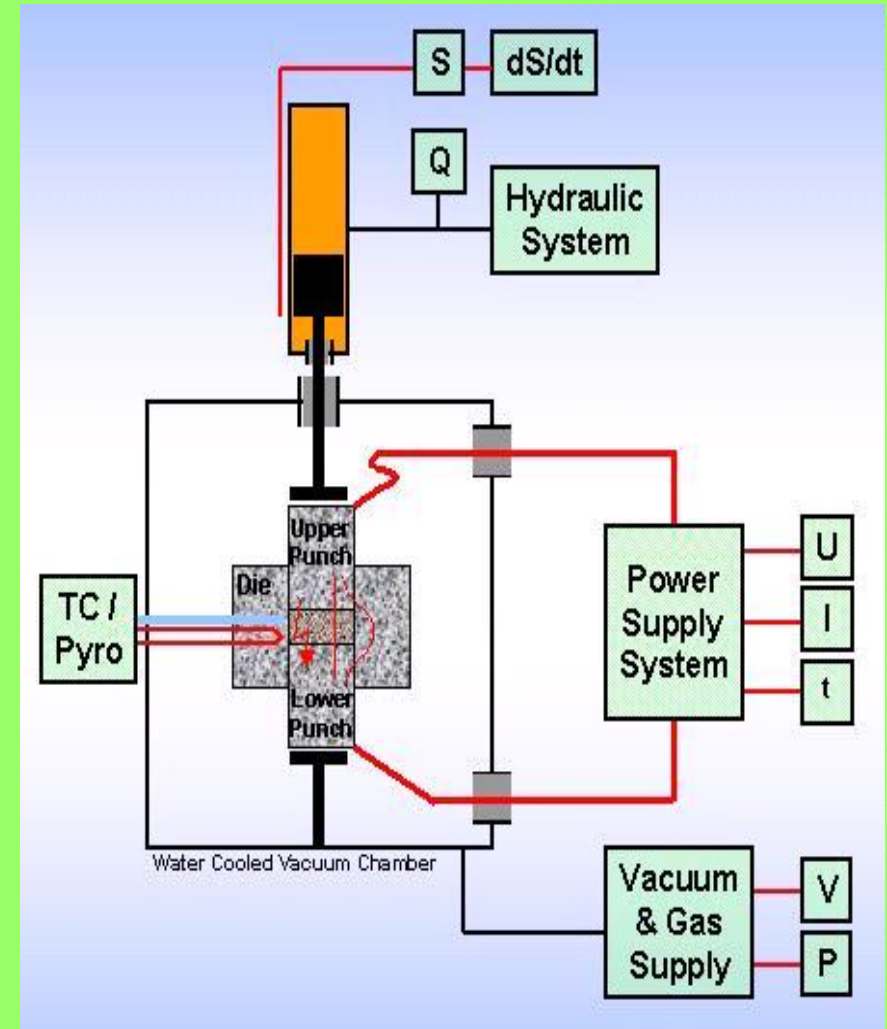
Outline

- **Introduction. Where this work was done?**
- **Why modeling is needed?**
- **Mathematical model of process.**
- **Input data.**
- **Contact resistances.**
- **Modeling examples. Conclusions.**
- **Outlook.**

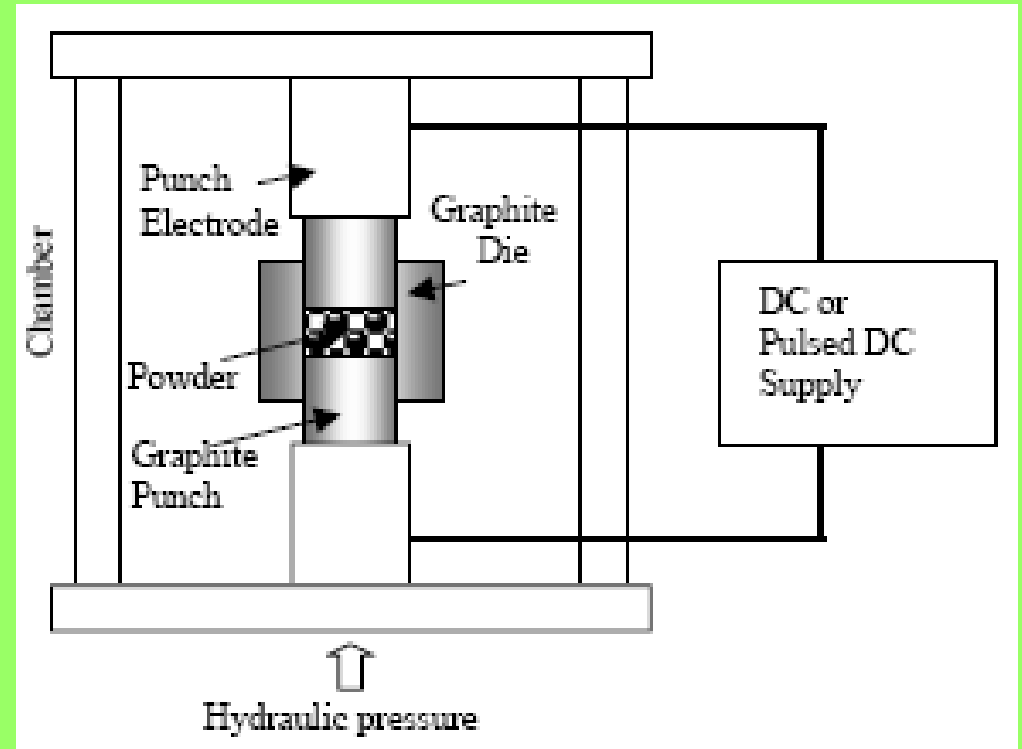
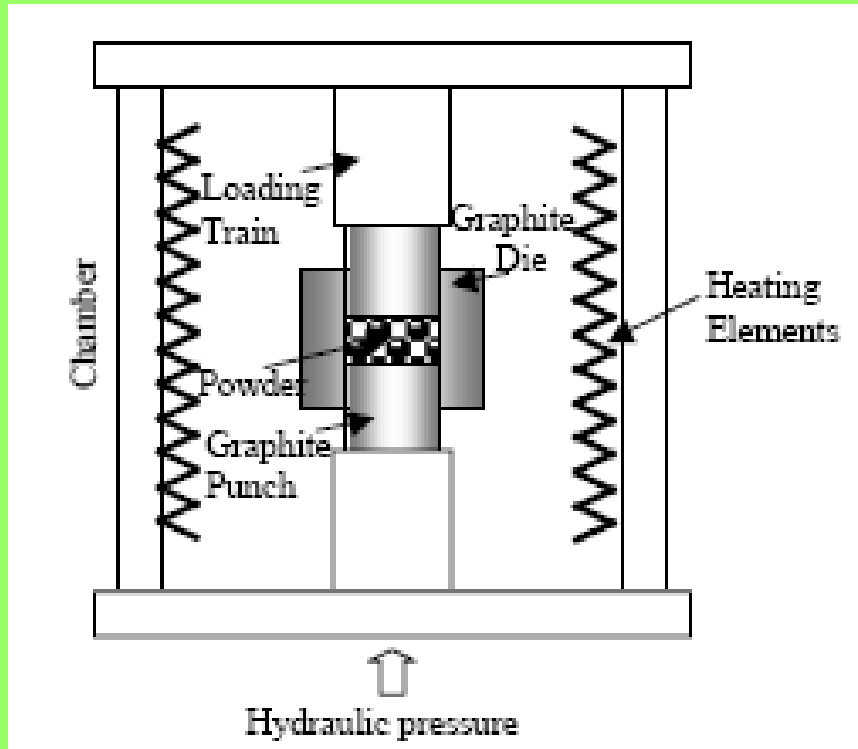
**What is meant by sintering with direct heating
by electric current ?**

Technology of sintering with direct heating by electric current

- Process of rapid consolidation of metallic, ceramic powders and composites into fully dense material – SPS, FAST, PECS
- Powder is loaded into a die, made from a conductive material (graphite, steel, ceramic), and consolidated by a combination of mechanical pressure and temperature produced by direct electrical (Joule) heating with the rates up to $1000^{\circ}\text{C}/\text{min}$.

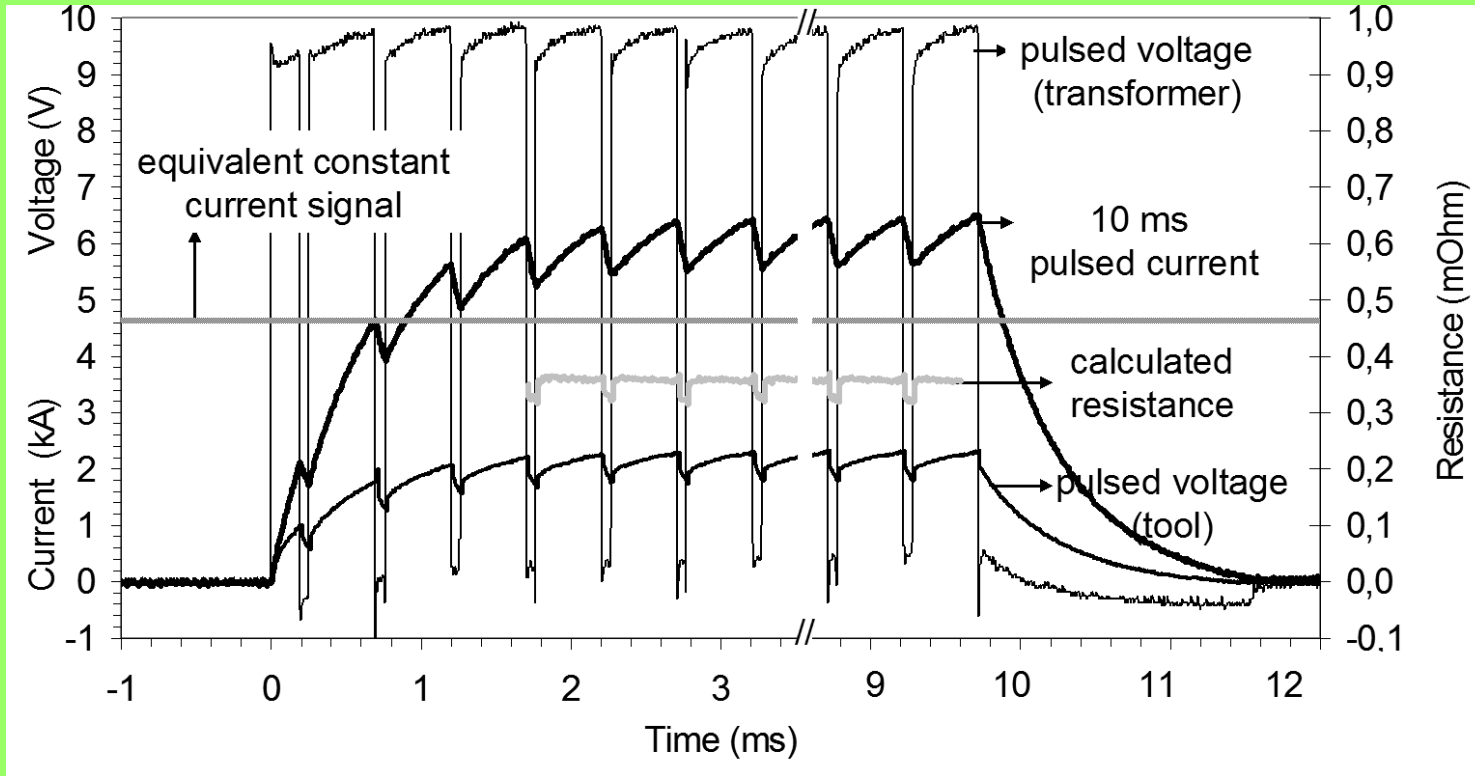


SPS vs Hot Pressing



Direct pulsed current

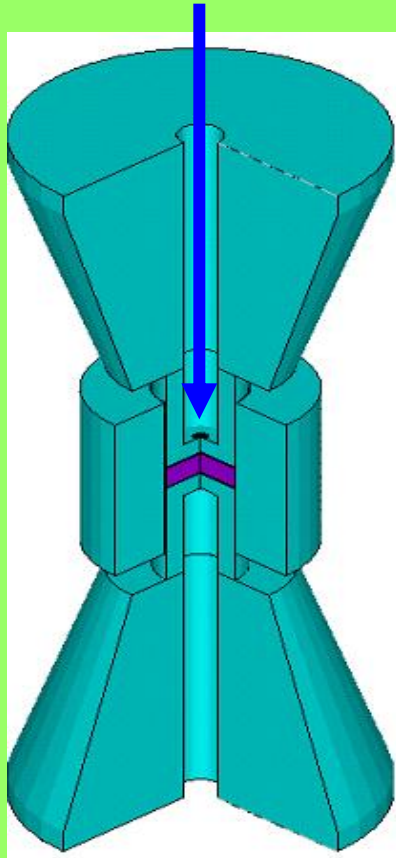
Pulse structure at Spark Plasma Sintering



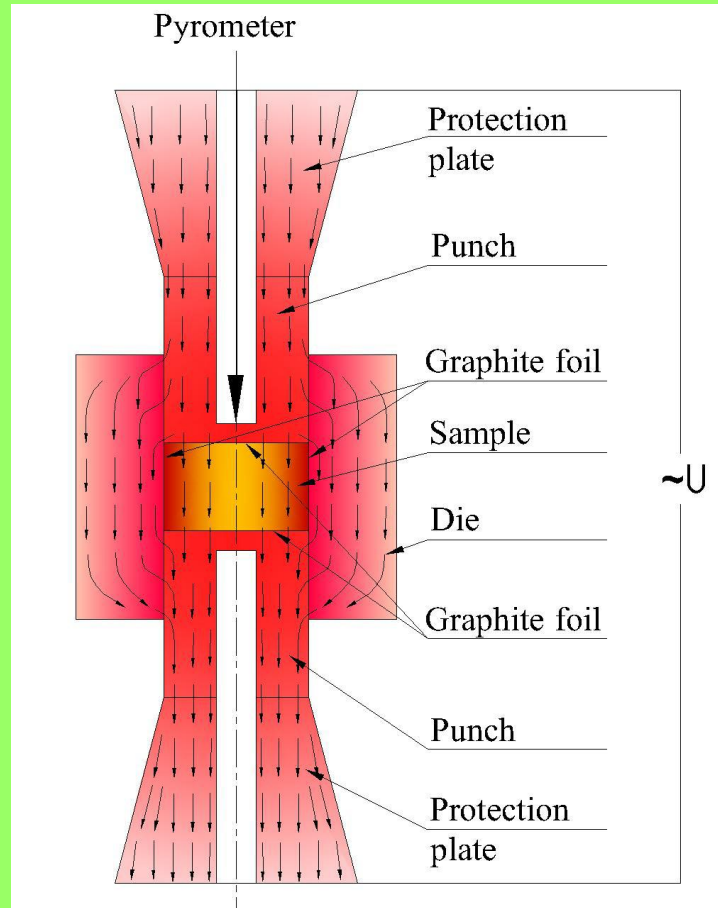
- Pulsed DC current
- Pulse time: 0-255 ms
- Pause time: 0-255 ms

Tool design and current paths during SPS

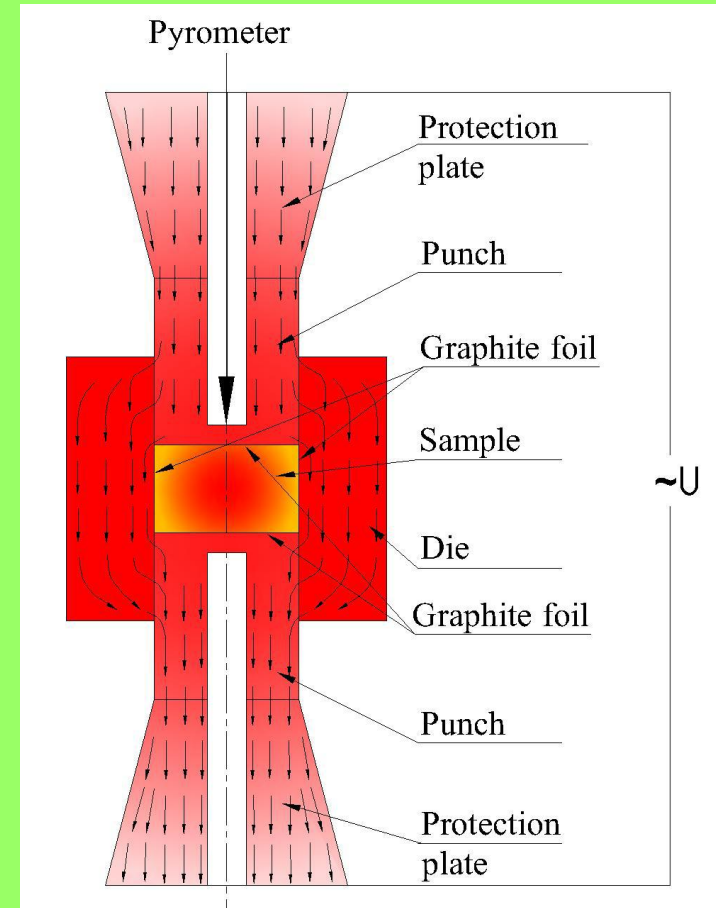
Pyrometer



Graphite tool



Conductive powder



Non conductive powder

Advantages of spark plasma sintering technique:

- a) very **quick consolidation** comparing with traditional hot pressing methods (HIP, HP)
 - ~ additional diffusion mechanisms
- b) possibility to **minimize grain growth**
 - ~ strength
- c) **Short processing time** (high heating rates, short dwell, fast cooling).
 - ~ productivity

😊 Consolidation of nanomaterials with improved properties within much shorter time periods

Problems using spark plasma sintering technique:

- a) temperature control within samples
- b) possible inhomogeneous temperature distribution (size and shape limitation)
- c) possible inhomogeneous distribution of density and other properties

Where this work was done?

1. **Donbass State Engineering Academy, Donbass, Kramatorsk, Ukraine**
Department of Materials Science, Department Materials Working by Pressure
2. **Katholieke Universiteit Leuven, Leuven, Flanders, Belgium**
Department of Metallurgy and Materials Engineering

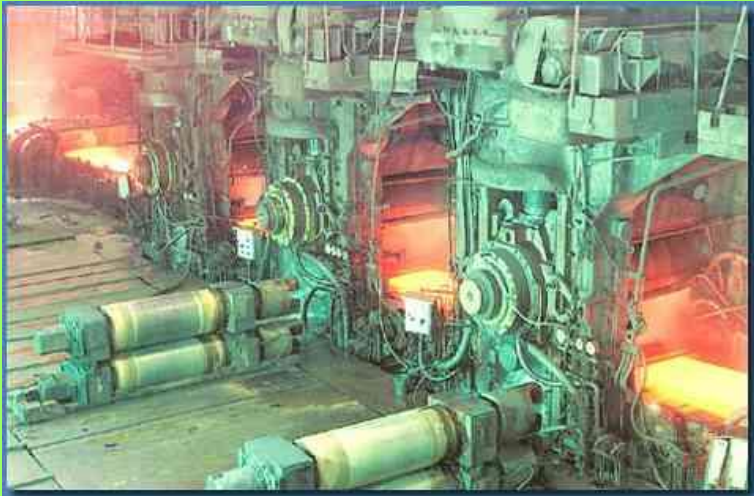


KU Leuven ★

★ **DSEA**

Kramatorsk on the map of Ukraine





Donbass State Engineering Academy



Kramatorsk – city in the south-east of Ukraine with population of 200 thousand people. Center of heavy machine building and ferrous metallurgy.



Donbass State Engineering Academy – High Education Institution of four level of accreditation.

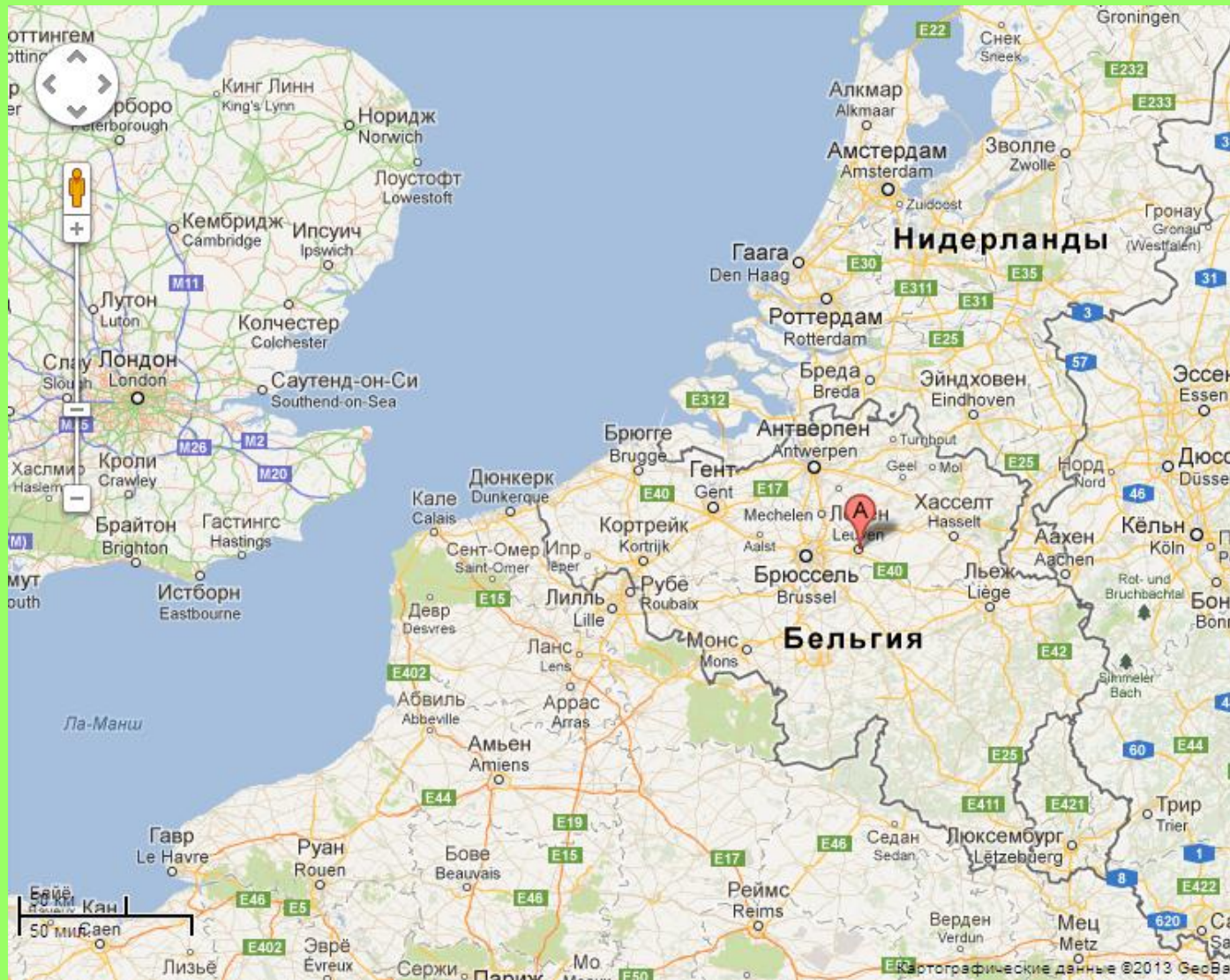
5390 full-time students. 5070 external students.

446 teachers, 250 associate professors, 19 full professors.



4 faculties, 40 departments. Education in mechanical engineering, metallurgical engineering, electrical engineering, IT, economics, management.

Leuven on the map of Belgium



Katholieke Universiteit Leuven



Leuven – city in the Flemish part of Belgium, located at 26 km on the east from Brussels. One of the university centers of Belgium. Main office of AB InBev (Stella Artois, Leffe, Hoegaarden)



Katholieke Universiteit Leuven – the oldest and the most famous university in Belgium. Founded in 1425 by Pope Martin V.

40.000 students, 3 groups of faculties: humanitarian sciences; biomedicine; science, engineering and technology. Place 58 in the Universities Word Ranking 2012/2013. Place 38 in the group of engineering and technology (Times, Thomson Reuters).



Department of Metallurgy and Materials Engineering. Group of Advanced Ceramics and Powder Metallurgy. Professor Jef Vleugels, Professor Omer Van der Biest, PhD Kim Vanmeensel.

Faculty of engineering sciences



SPS (FAST) installation in KU Leuven



HP D 25/1 FCT Systeme (Rauenstein, Германия)

Temperature: 20-2200 °C

Load: 5-250 кН

Heating rate:
5-400 °C /min

Power: 8 kW

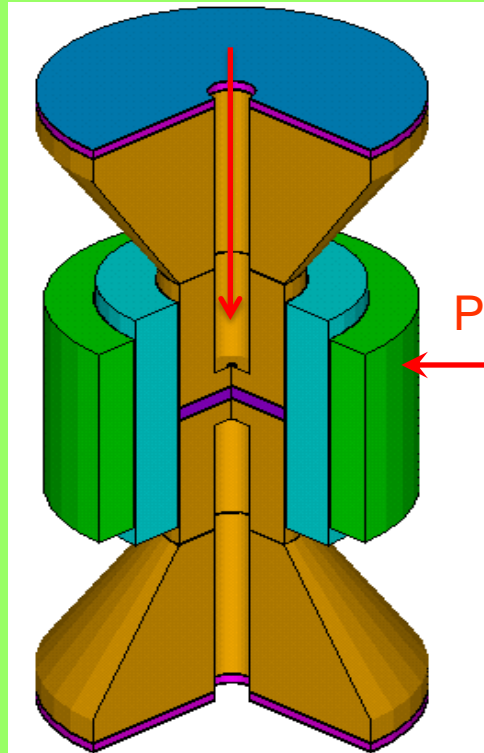
Pulse: 0-255 мс

Diameter of compact
(max): 80 мм

Atmosphere: vacuum, Ar,
N₂, He

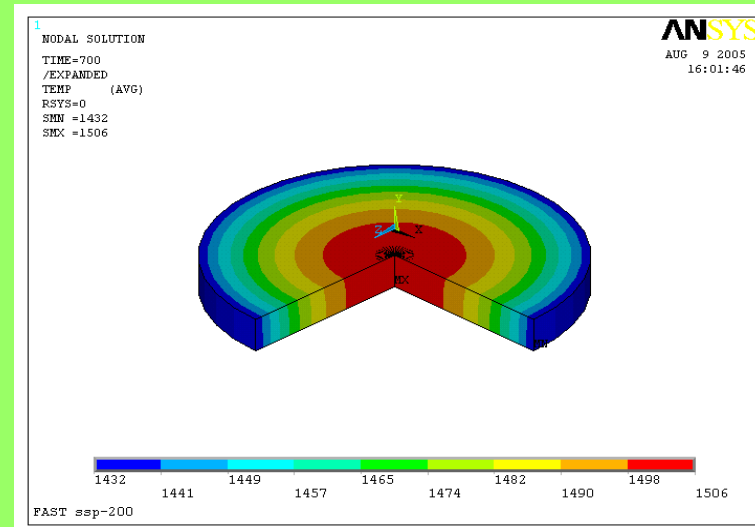
Why modeling is needed?

Pyrometer № 2

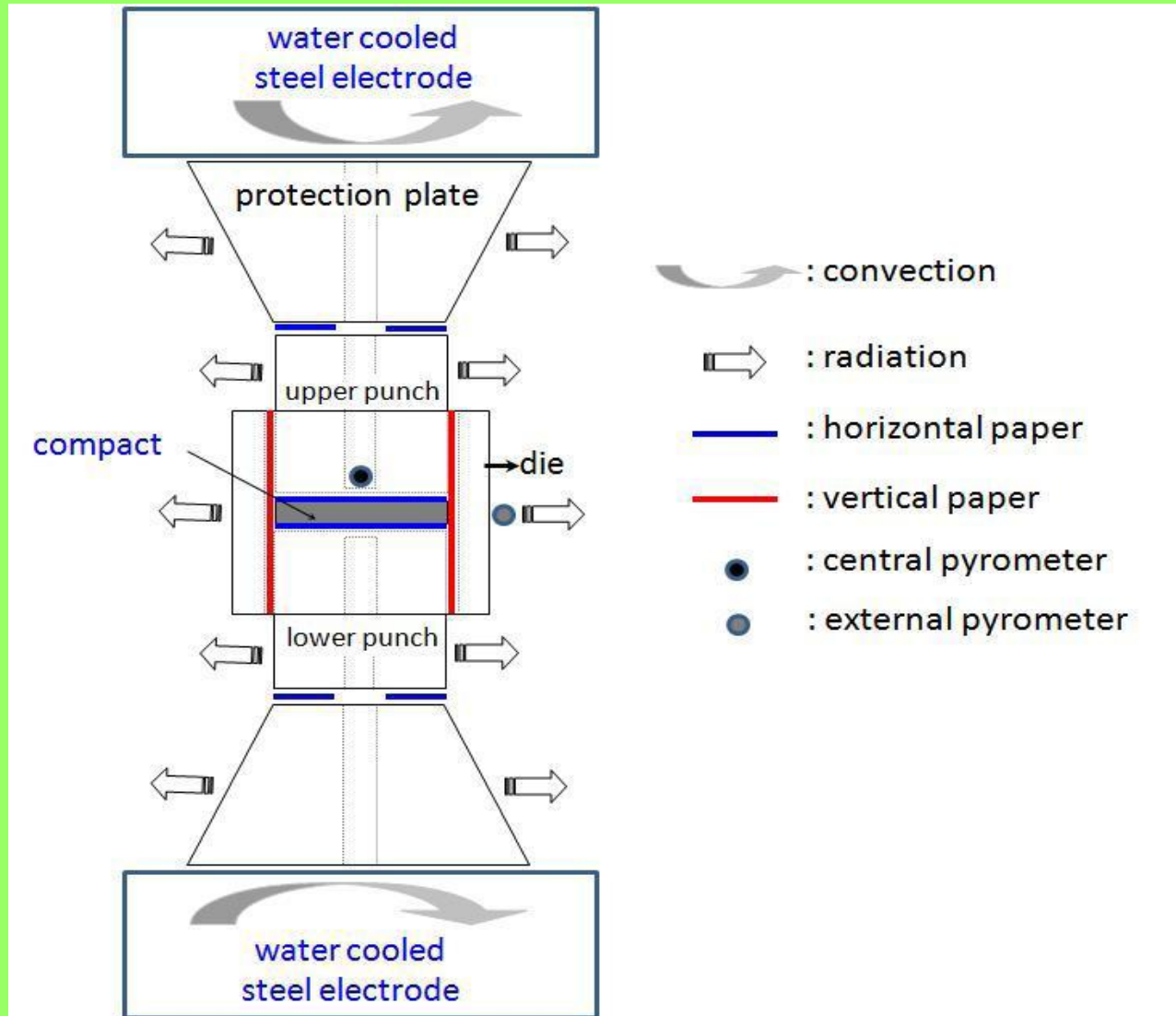


Pyrometer № 1

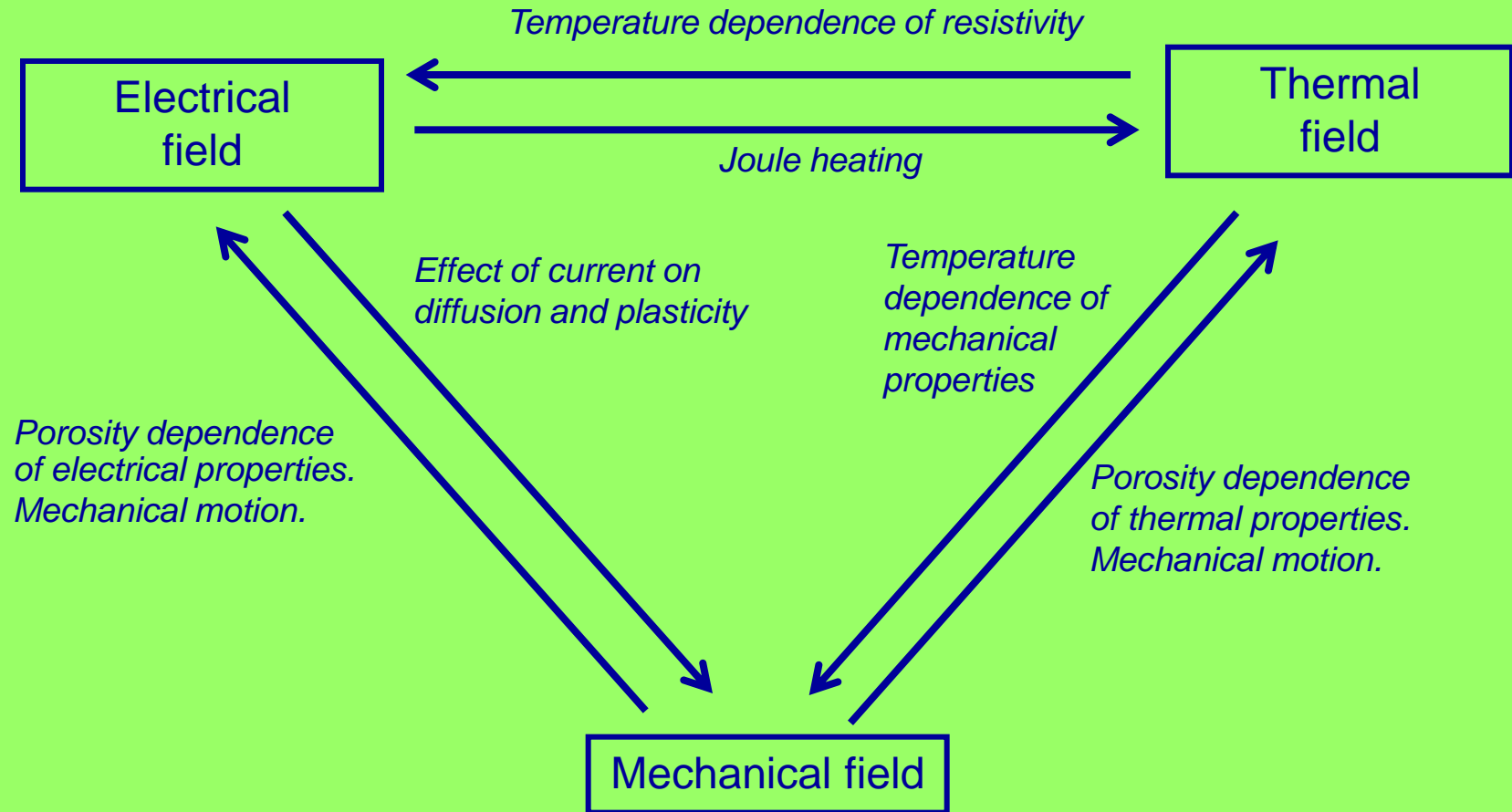
- Temperature control (especially at high heating rates)
- Temperature distribution (especially for large parts and in the case of narrow temperature window)
- Properties distribution (particularly density)
- Shape distortion (during plastic deformation)



Schematic view of tool



Physical fields, interacting during sintering with direct electrical heating



Mathematical model of process

Electrical field

Ohm's law

$$\vec{j} = \sigma(\rho, T) \cdot \vec{E}$$

Joule's law

$$w_j = \vec{j} \cdot \vec{E} = \sigma(\rho, T) \cdot \vec{E}^2$$

Thermal field

Fourier's law

$$\gamma \cdot c(\rho, T) \cdot \frac{\partial T}{\partial t} = \lambda(\rho, T) \cdot \nabla^2 T + w_j$$

Stefan–Boltzmann law

$$w_r = \sigma_s \cdot \varepsilon(T) \cdot (T_e^4 - T_a^4)$$

Mechanical field

Hook's law

$$T_\varepsilon = \frac{1}{3K(\rho, T)} \cdot T_{\sigma_0} + \frac{1}{2G(\rho, T)} \cdot D_\sigma$$

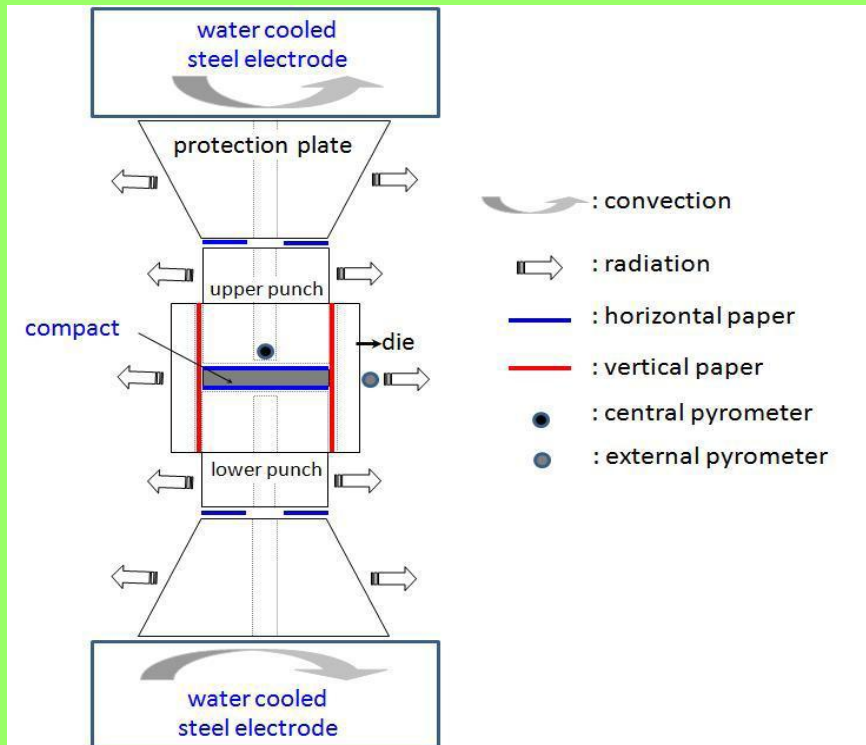
Constitutive equations

$$T_\varepsilon = F(T_\sigma, \rho, T, H)$$

$$\dot{\varepsilon}_{eff} = A_0 \frac{\sigma_{eff}^n}{d^p} \exp\left(-\frac{Q}{RT}\right)$$

Mathematical model of process

Contact properties



Thermal conductivity

$$w_c = \lambda_c(T) \cdot (T_1 - T_2)$$

Electrical conductivity

$$\vec{j}_c = \sigma_c(T) \cdot (\vec{U}_1 - \vec{U}_2)$$

Heat generation

$$w_c = \sigma_c(T) \cdot \vec{U}^2$$

Convection

$$w_{conv} = h(T) \cdot (T_p - T_w)$$

Friction law (Coulomb)

$$f = \mu \cdot F_n$$

Input data

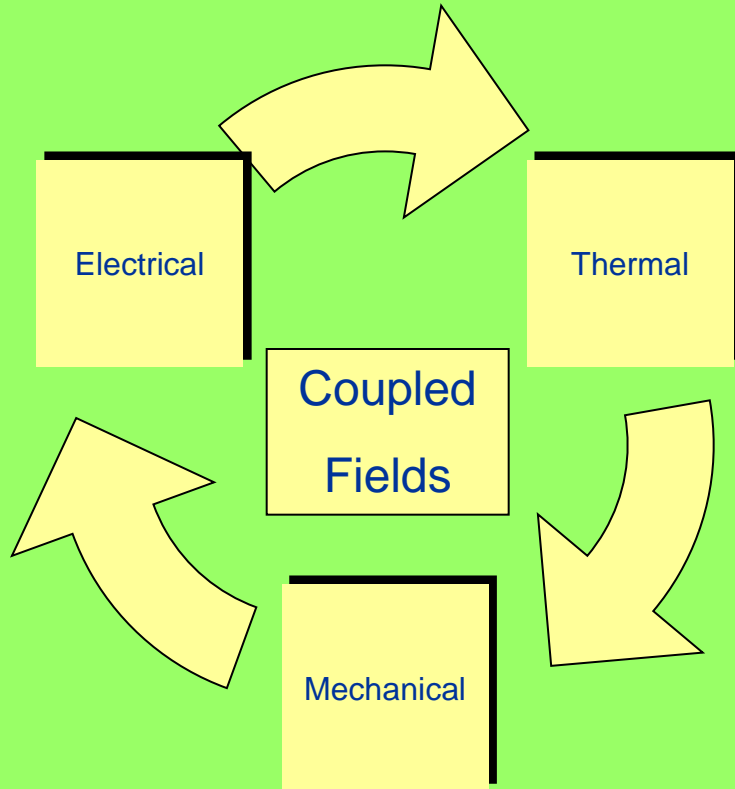
Properties of tool and sample materials in dependence on temperature and porosity

1. Electrical conductivity
2. Specific heat
3. Thermal conductivity
4. Thermal expansion coefficient
5. Mechanical properties (Young's modulus, Poisson coefficient etc.)

Contact properties (vertical and horizontal)

1. Specific electrical conductivity
2. Specific thermal conductivity
3. Radiation coefficient
4. Convection coefficient
5. Friction coefficient

FEM software used for modeling



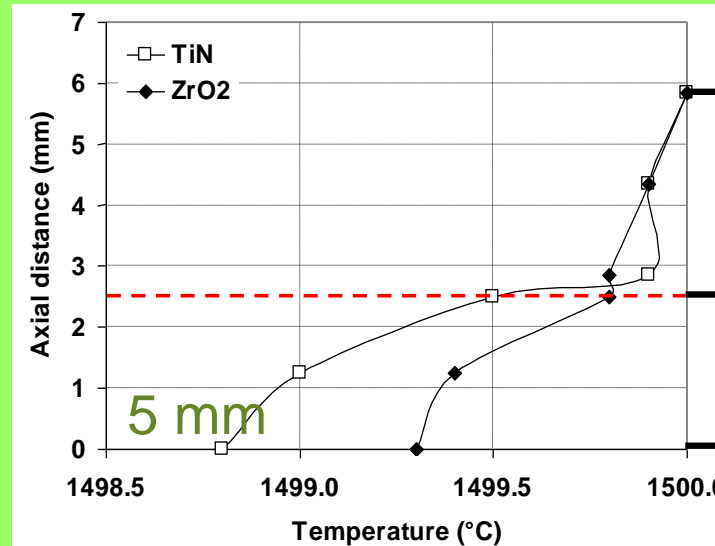
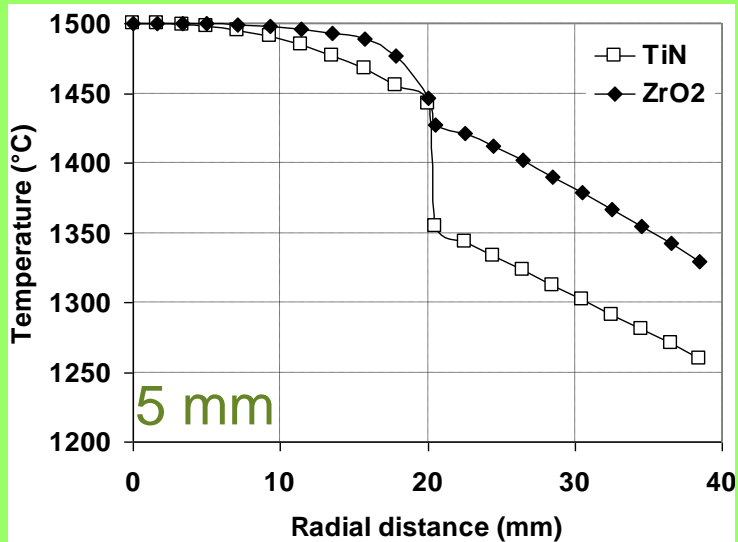
ANSYS и ABAQUS software provide coupling of electrical and thermal fields
or thermal and mechanical fields separately 😞

Modeling of temperature field

K. Vanmeensel, A. Laptev, J. Hennicke , J. Vleugels,
O. Van der Biest

Acta Materialia 53 (2005) 4379–4388

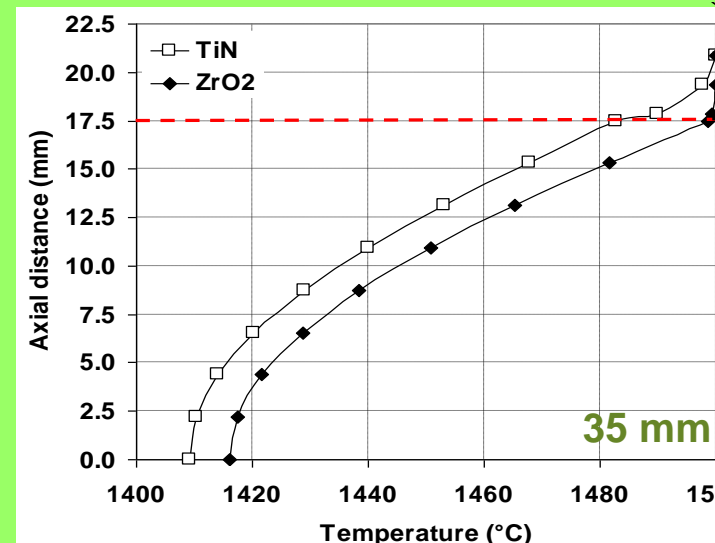
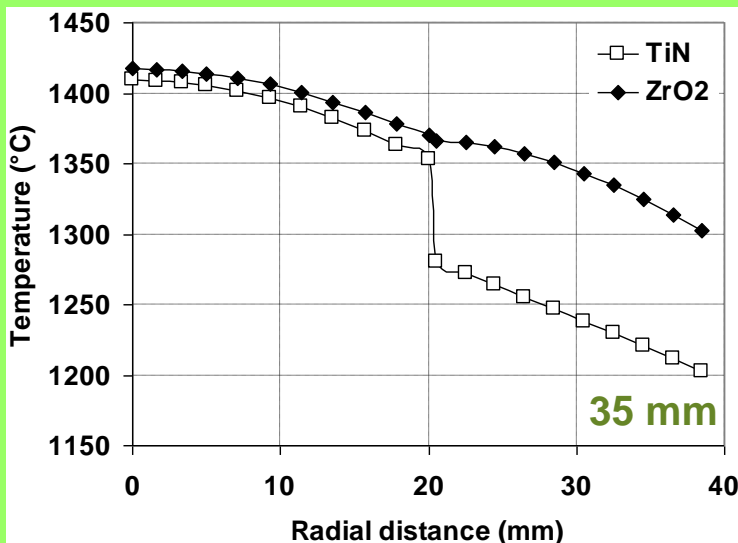
Temperature distribution in sample and in tool



Pyrometer

Sample top

Sample centre

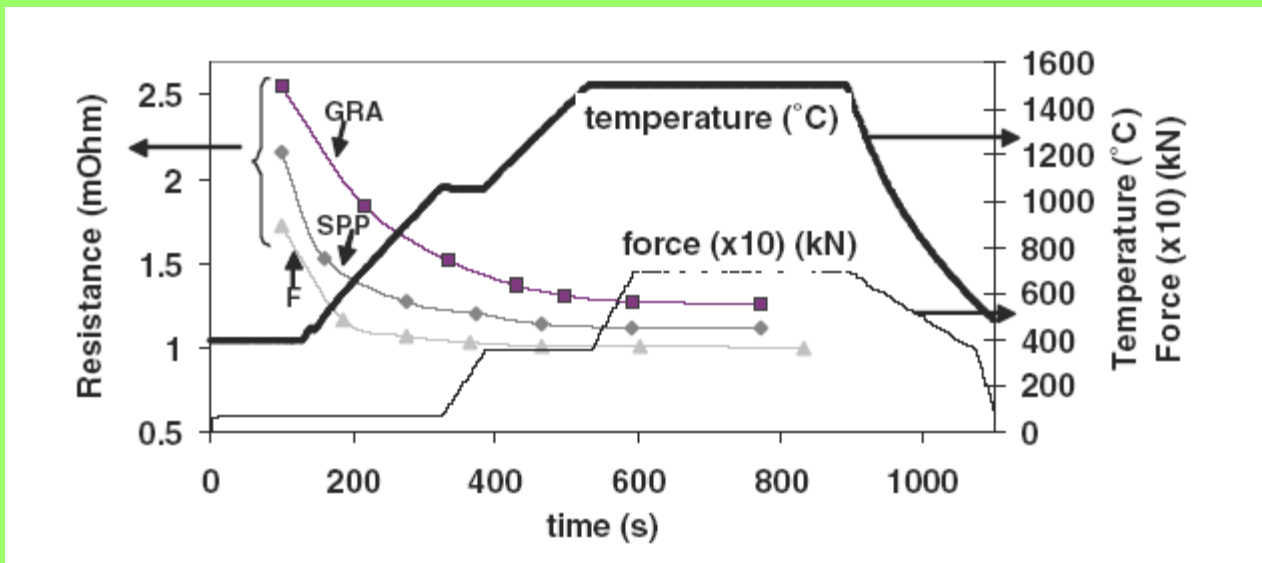
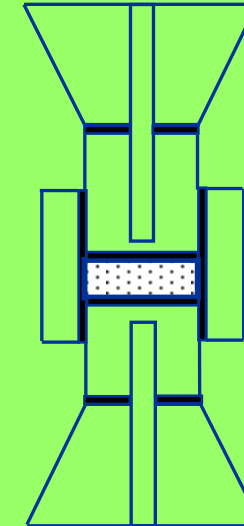
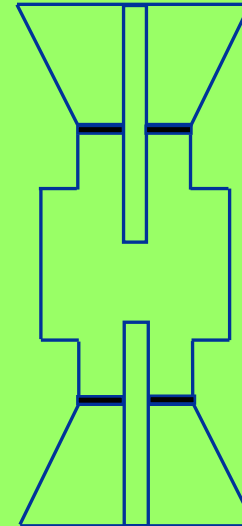
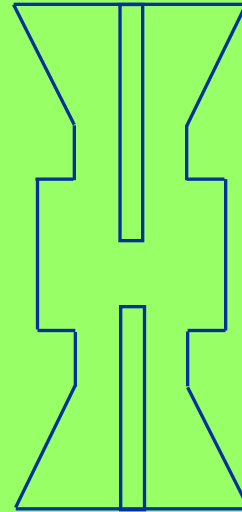
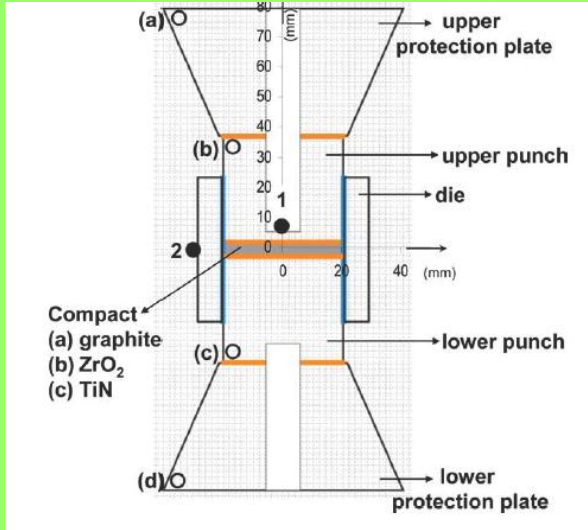


Pyrometer

Sample top

Sample centre

Investigation of contact resistances

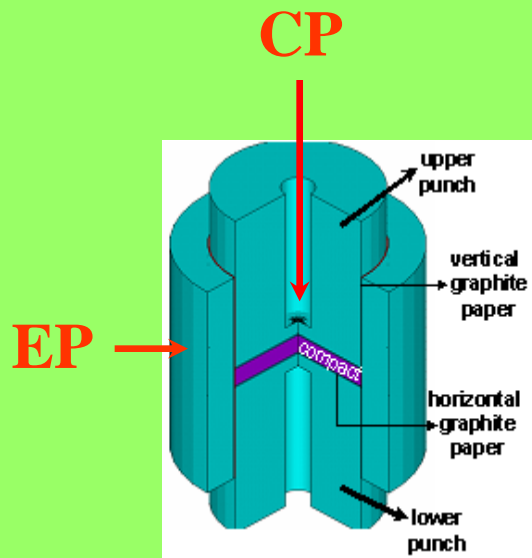


$$I_c = I_p \sqrt{\frac{2}{3}}$$

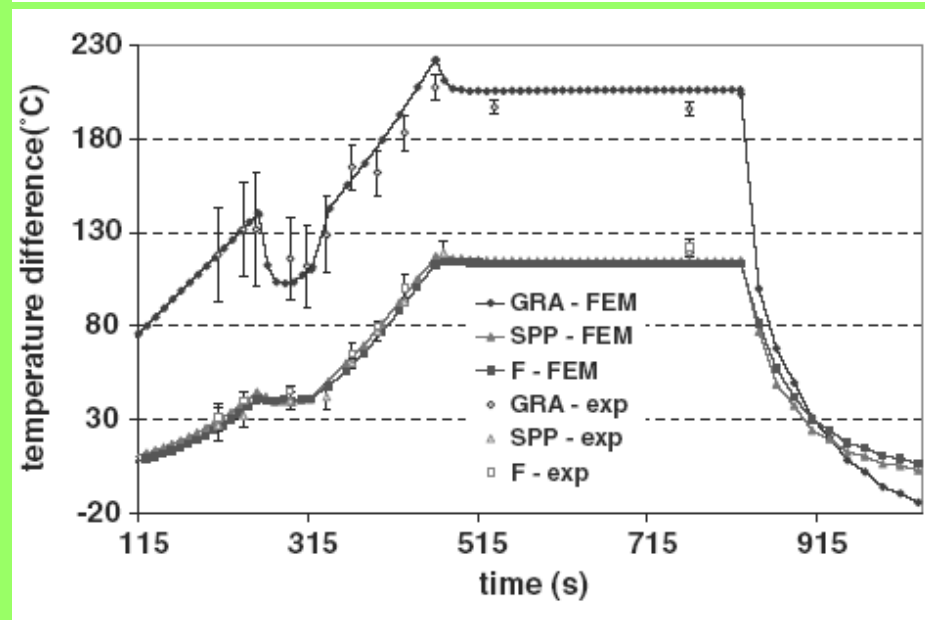
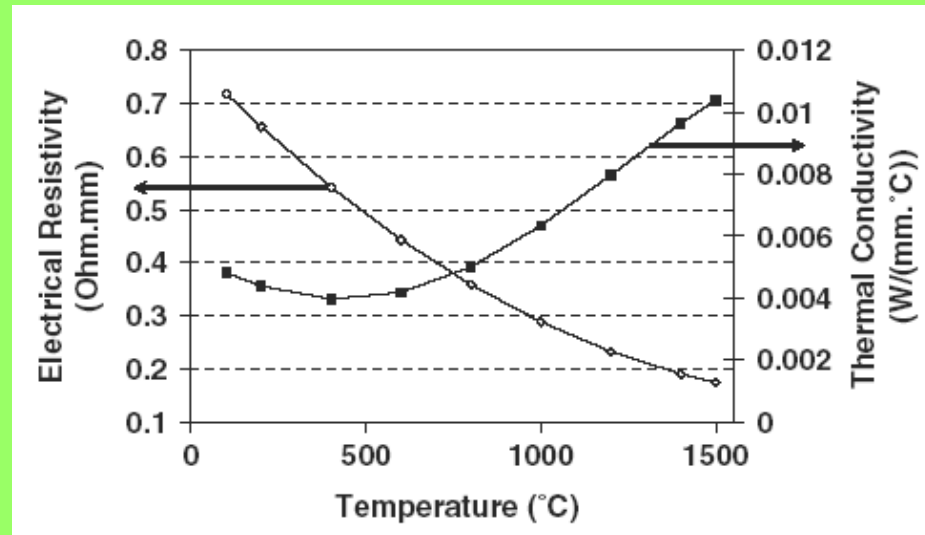
Investigation of contact resistances

$$\lambda_p = \eta \cdot \lambda_{gr} \cdot \frac{\rho_{gr}}{\rho_p} \quad \eta = 2.85$$

Resistance of vertical contacts approximately 7 times larger than horizontal contacts.

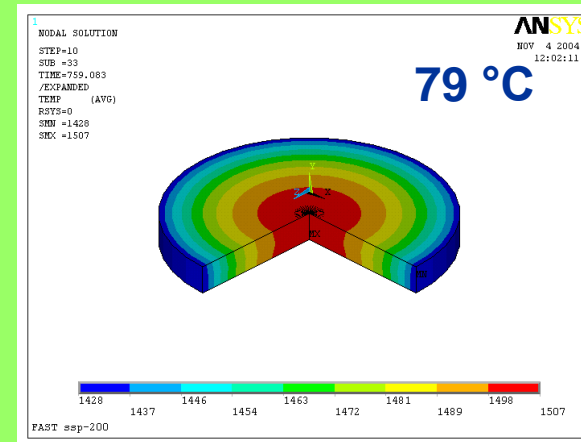
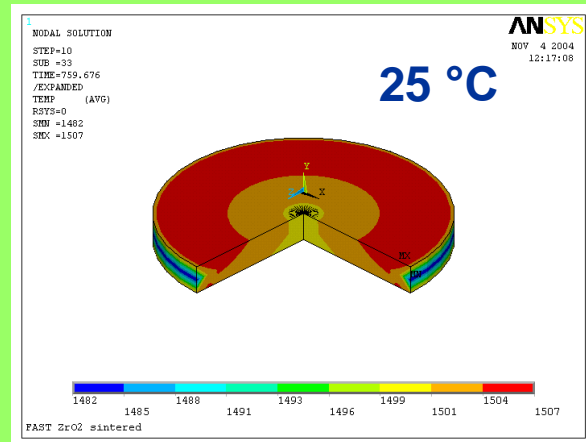
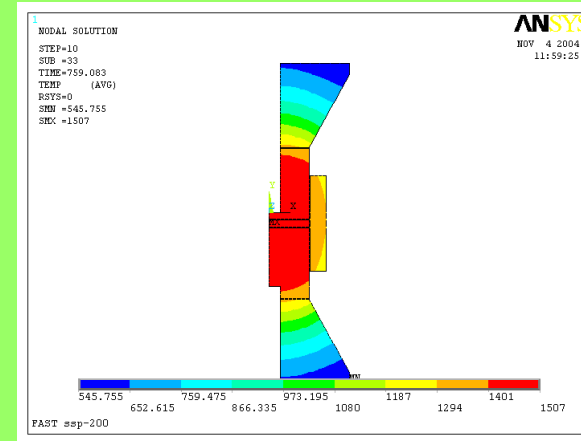
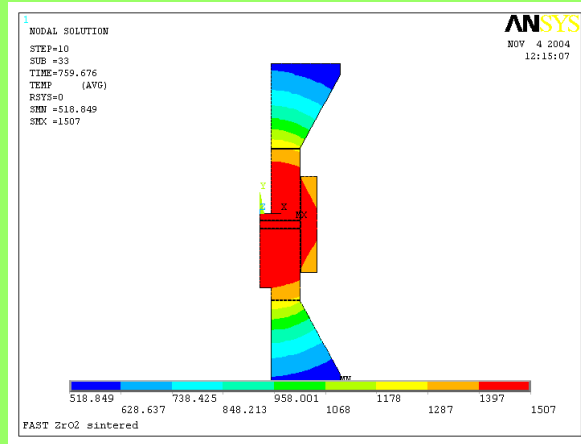


Vertical resistances have an essential influence on temperature distribution.



Holding at 1500°C

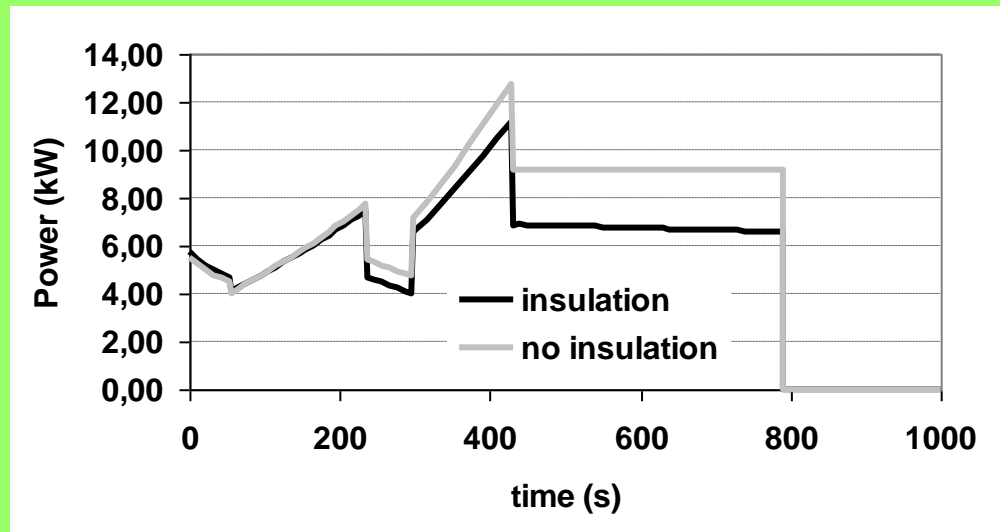
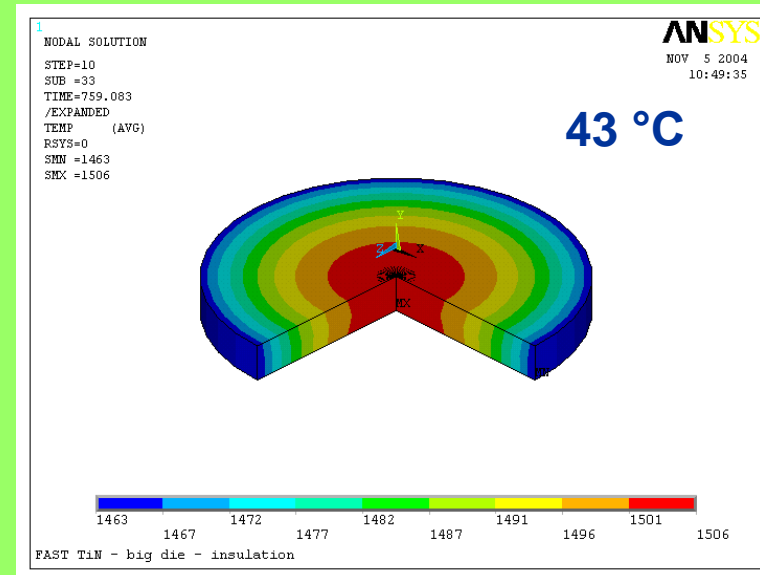
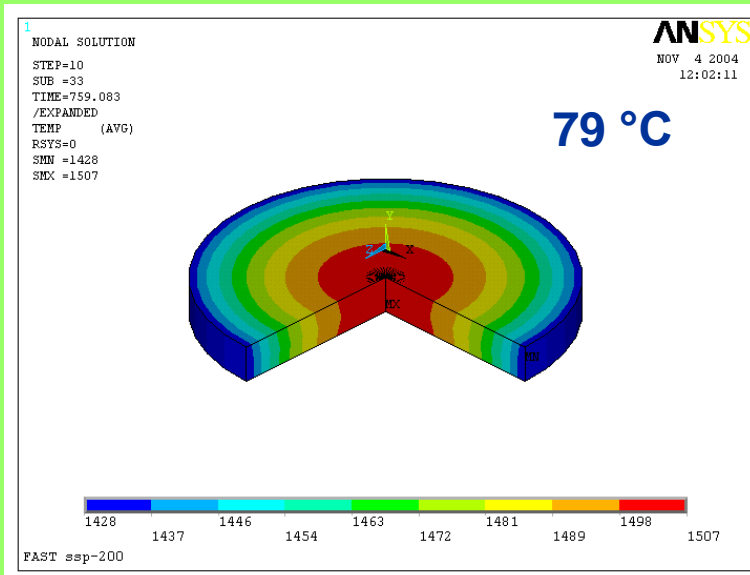
Influence of samples conductivity on temperature distribution at 1500°C



3Y-ZrO₂

TiN

Influence of die insulation at 1500°C



Main conclusions (section # 1)

- **Temperature distribution during SPS within both tool and sample can be very inhomogeneous. Therefore a special attention must be paid to correct temperature control.**
- **Contact resistances have essential influence on temperature distribution in both tool and sample during SPS.**
- **Conductivity of sample material and die wall thickness determine character of temperature distribution within the sample.**
- **Application of thermal insulation results in essential decrease of temperature gradient and energy consumption during SPS.**

Spark Plasma Sintering of ZrO_2 -TiCN (60/40) composite

K. Vanmeensel, A. Laptev, O. Van der Biest, J. Vleugels
Journal of European Ceramics Society 27 (2007) 979–985

Powder composite ZrO₂-TiCN (60/40)

Y-ZrO₂

- High toughness (10 MPa.m^{1/2})
- High strength (1.2 GPa)
- Moderate hardness (12 GPa)
- Electrically insulating

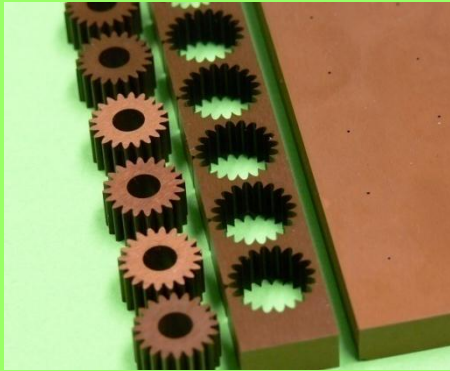
TiN

- Low toughness (3.5 MPa.m^{1/2})
- Low strength (0.5 GPa)
- High hardness (17 GPa)
- Electrically conductive

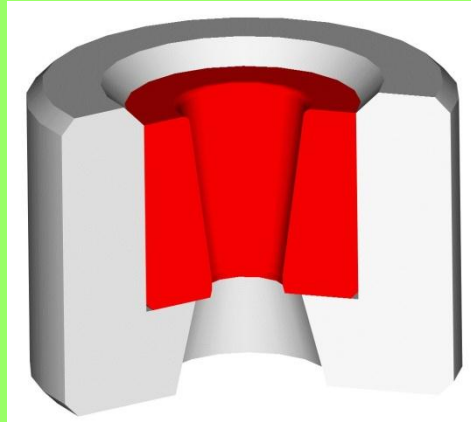


ZrO₂-TiN (60/40)

ZrO₂-TiCN components manufactured by EDM



Gears



Extrusion die



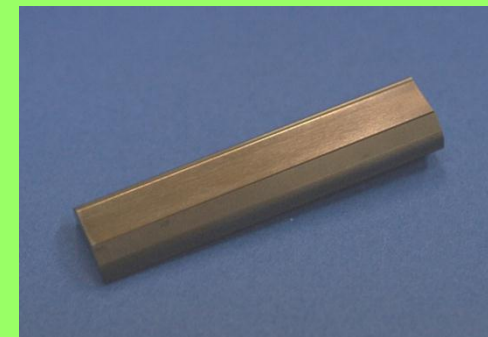
Attritor disc



Gears

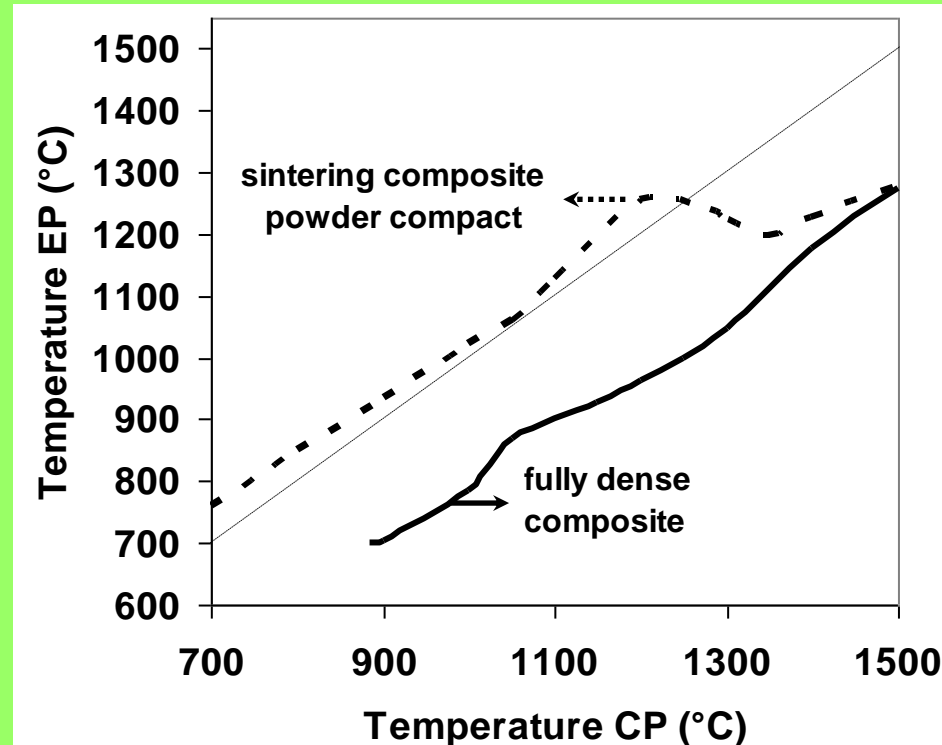
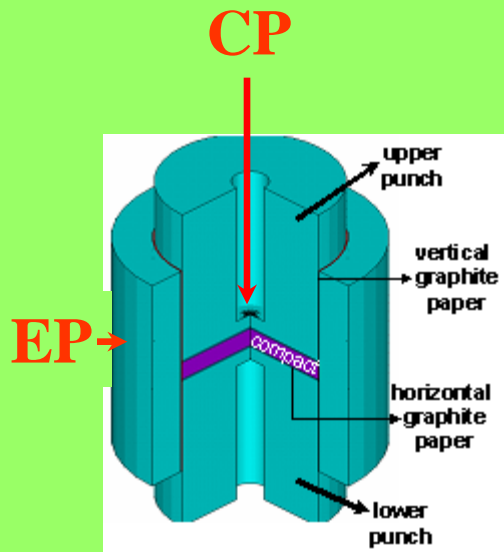


Dies



Punching tool

Development of temperature field during consolidation



Dense composite: $T_{\text{die}} \ll T_{\text{compact}}$

Porous composite: $T < 1250^{\circ}\text{C}$: $T_{\text{die}} \sim T_{\text{compact}}$ $T > 1250^{\circ}\text{C}$: $T_{\text{die}} \ll T_{\text{compact}}$

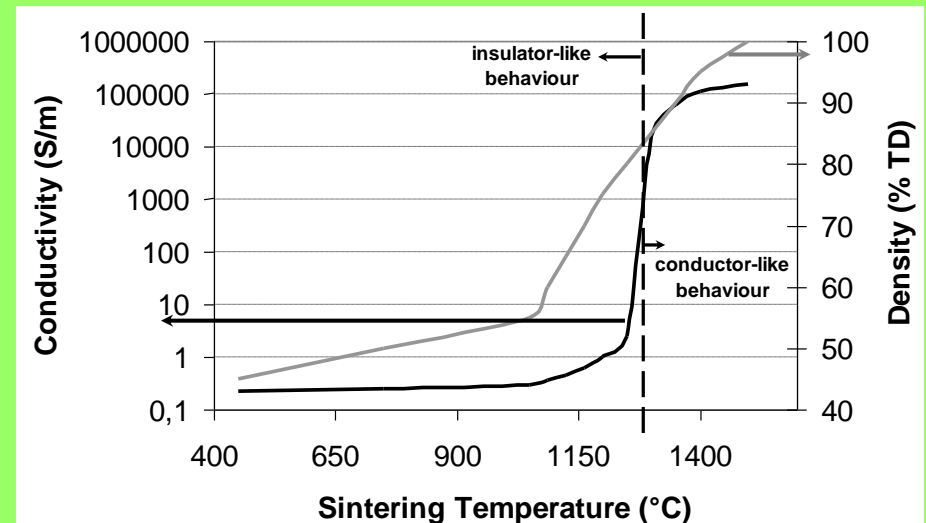
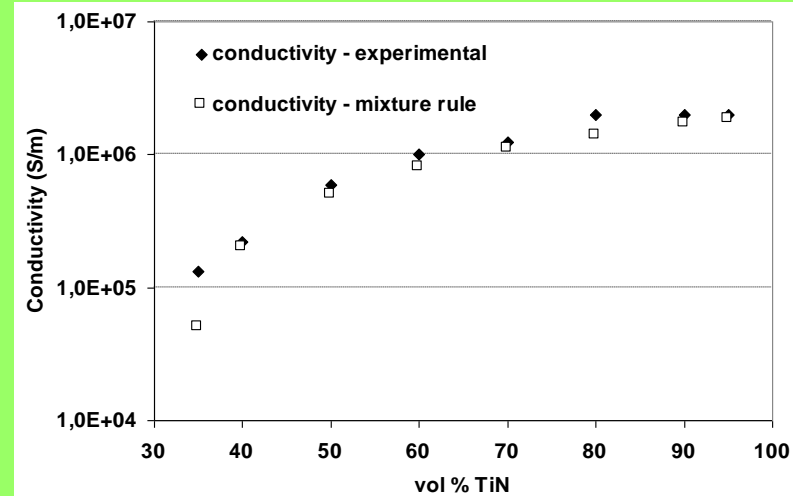
Influence of composition and porosity on properties

*Influence of composition
(Polder – Van Santen mixture rule)*

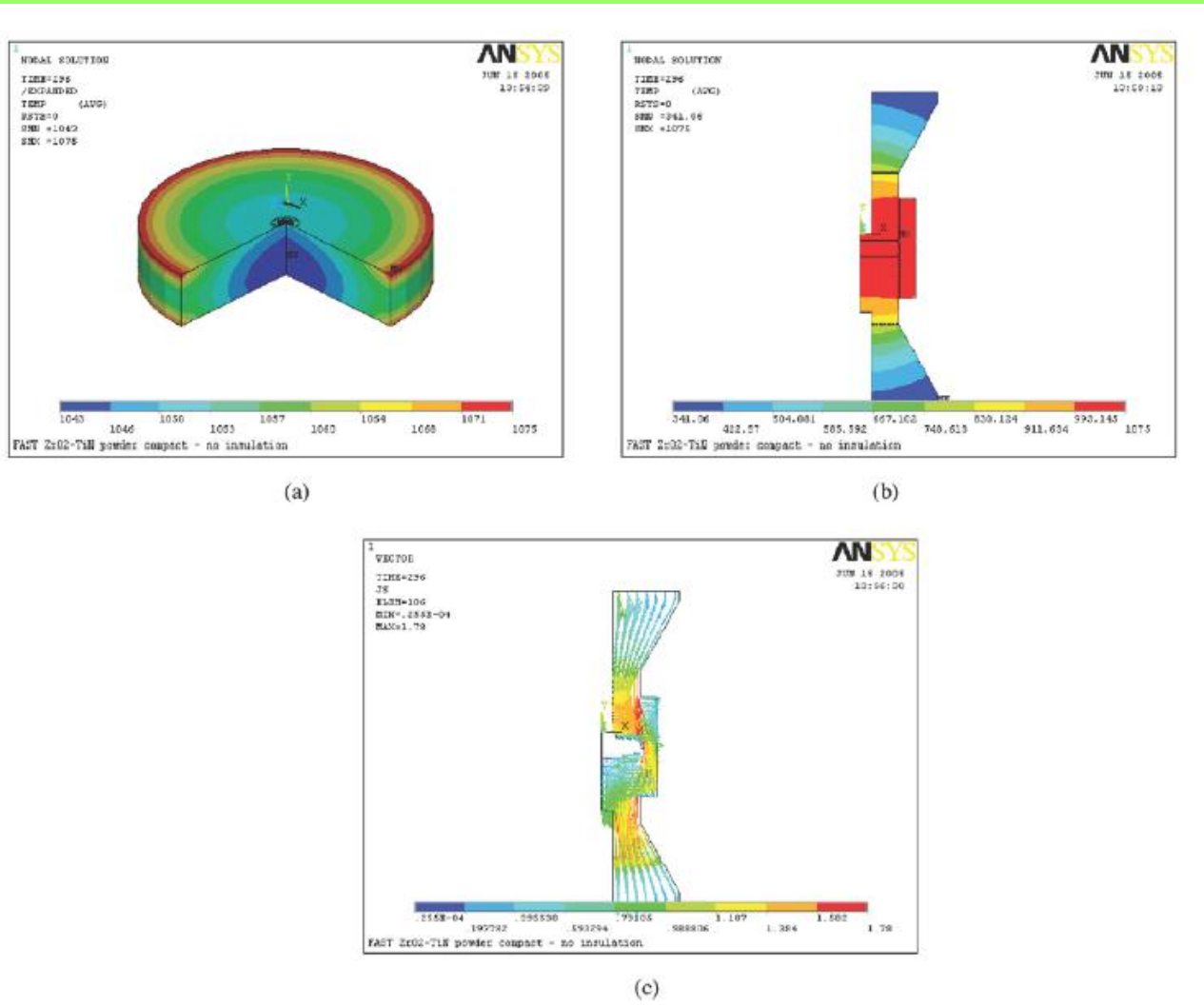
$$\rho_c = \rho_{ZrO_2} + (\rho_{TiN} - \rho_{ZrO_2}) \frac{V_{TiN} \rho_c}{\rho_c + \frac{\rho_{TiN} - \rho_c}{3}}$$

*Influence of porosity
(formulae Argento – Bouvard)*

$$k_{eff} = k_s \left(\frac{\rho - \rho_0}{1 - \rho_0} \right)^{t(1 - \rho_0)}$$



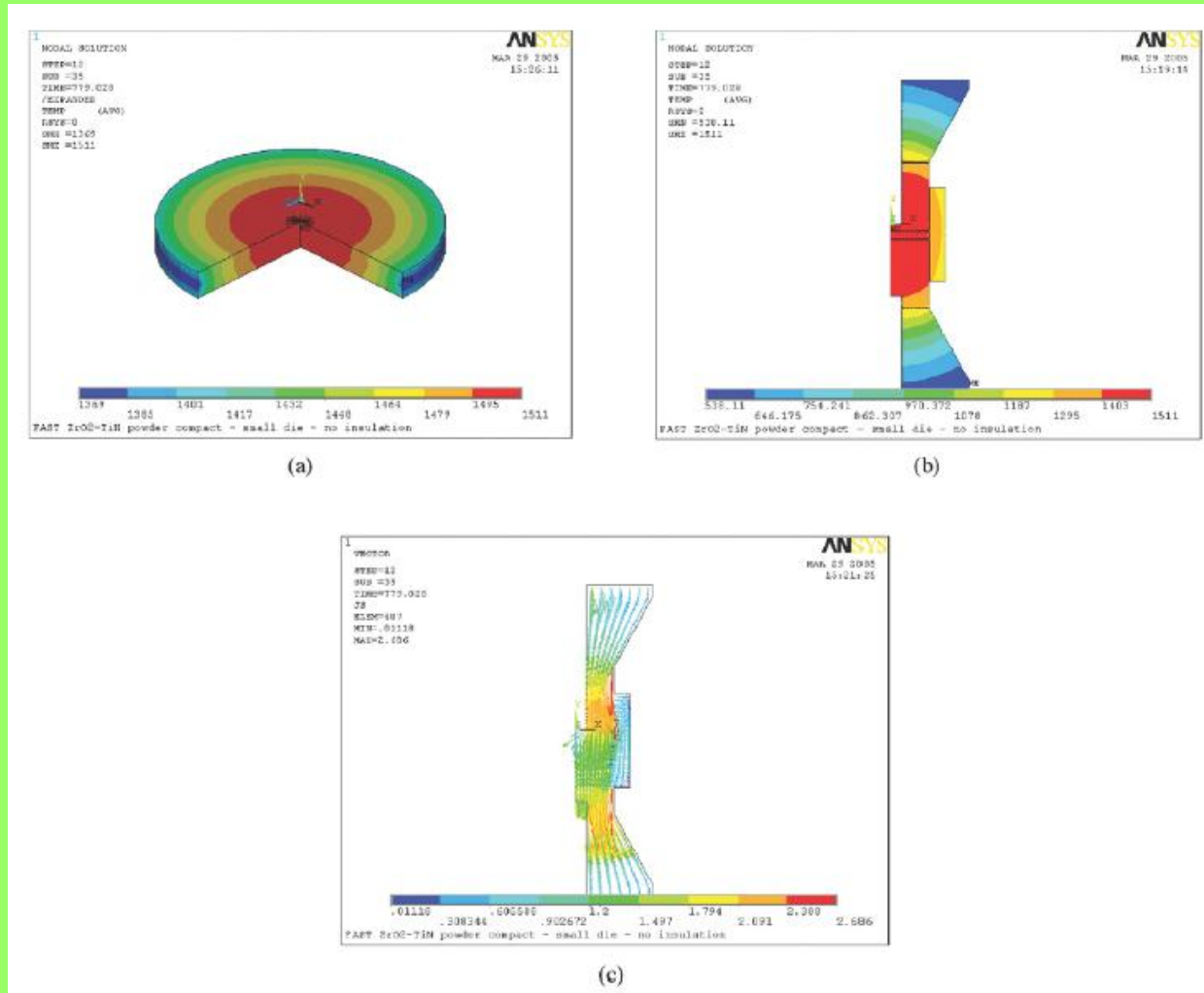
Temperature and current distribution at 1050°C



D=40 mm

$\Delta T_{max}=52^{\circ}\text{C}$

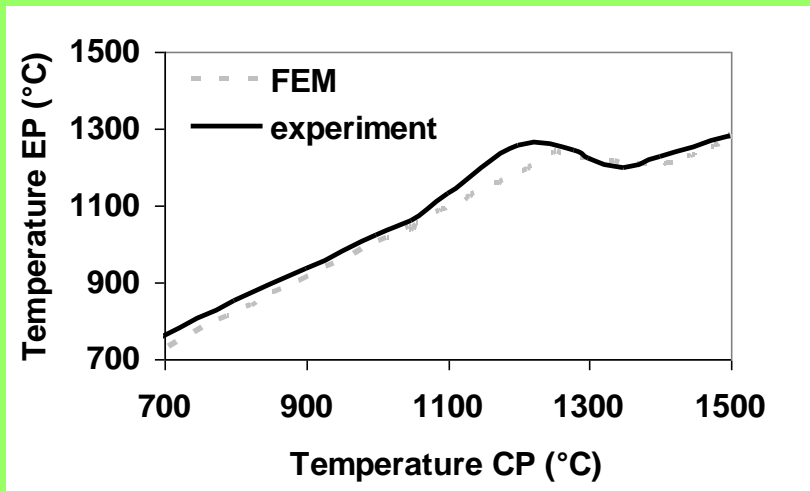
Temperature and current distribution at 1500°C



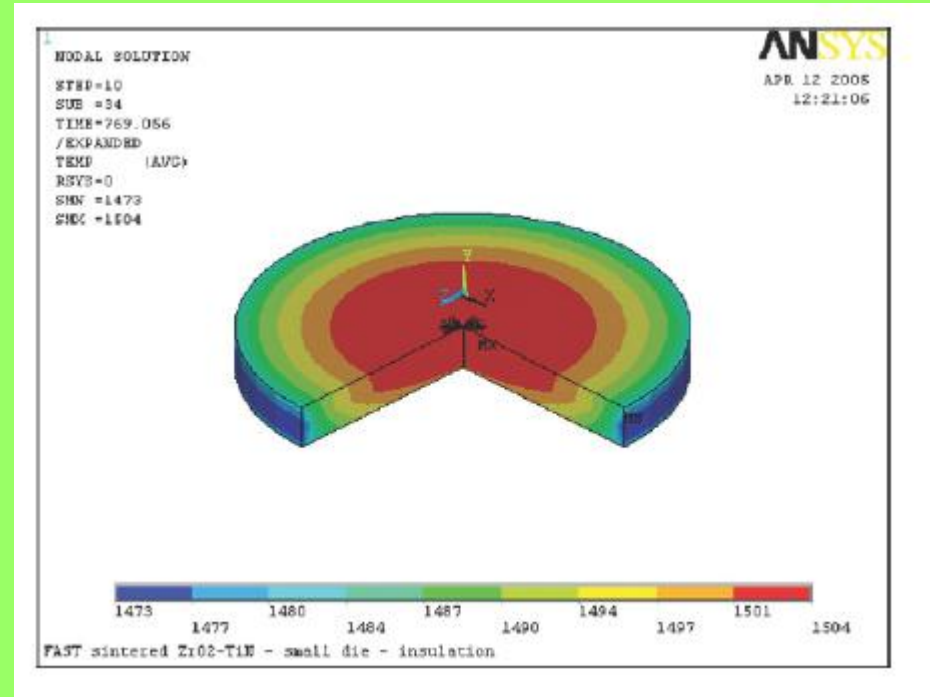
D=40 mm

$\Delta T_{max}=142^{\circ}\text{C}$

Accuracy of modeling and influence of thermal insulation



Modeling results vs pyrometers reading



Temperature distribution when thermal insulation of die is used. $\Delta T_{max}=31^{\circ}\text{C}$

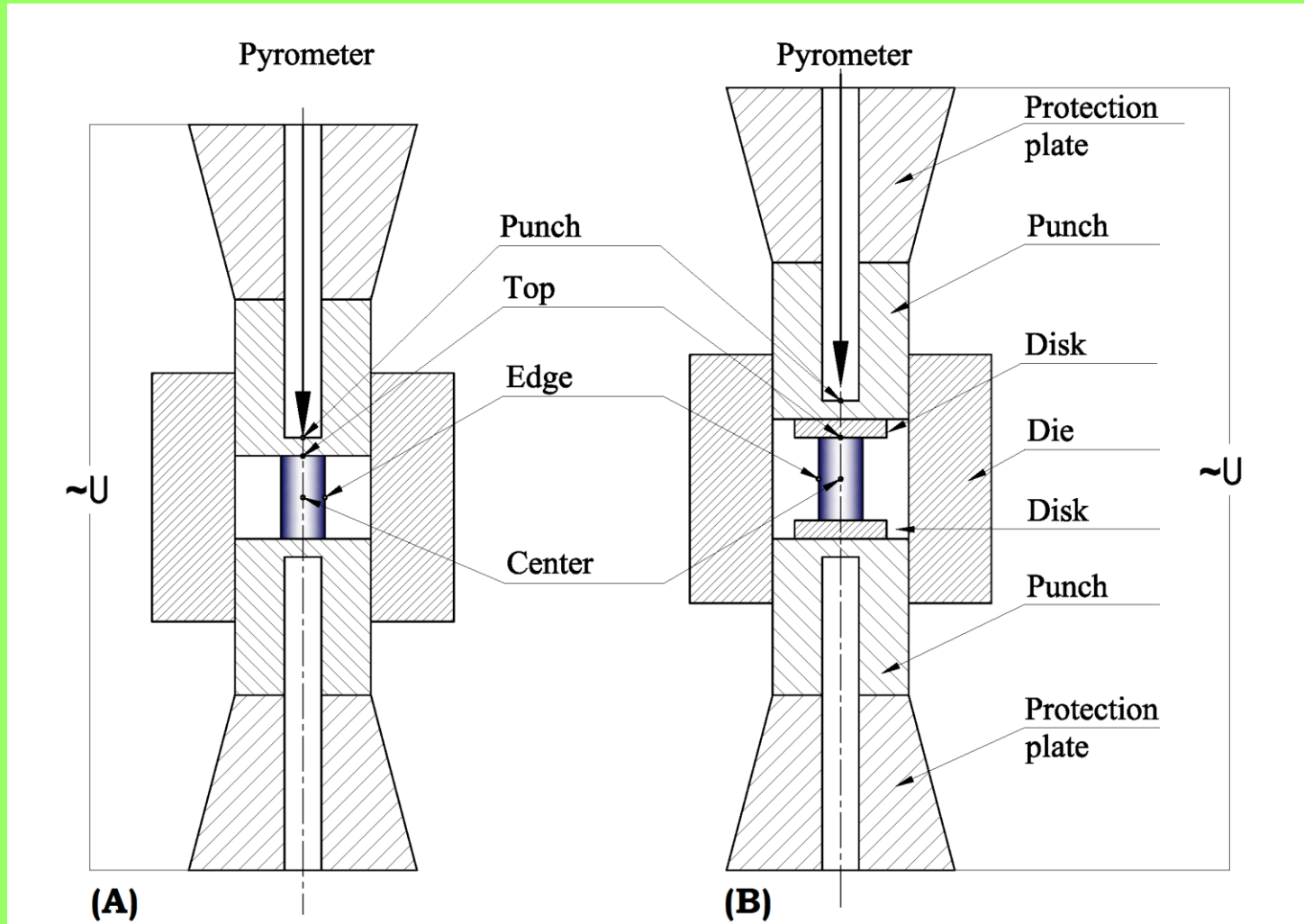
Main conclusions (section # 2)

- The application of ceramics powder mixtures containing a conductive phase allows Spark Plasma Sintering of materials suitable for Electrical Discharge Machining.
- During sintering the conductivity of such composite material can be drastically reduced due to decrease of porosity. The Polder – Van Santen and Argento – Bouvard relationships can be used for modeling of conductivity change.
- FEM analysis has shown that application of thermal insulation results in an essential reduction of temperature gradient within a sample.

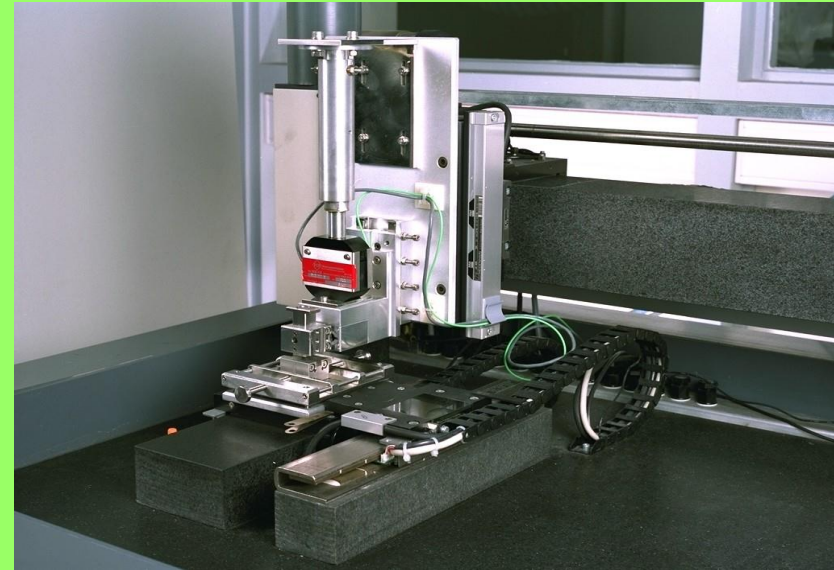
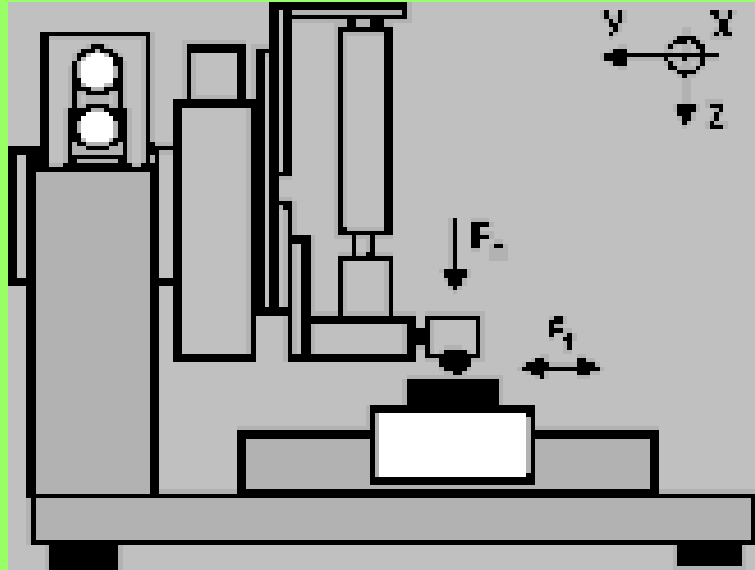
Plastic deformation of ceramics

K. Vanmeensel, A. Laptev, H. Sheng, I. Tkachenko,
O. Van der Biest, J. Vleugels
Acta Materialia 61 (2013) 2376–2389

Two tool setups used in experiments



Measurement of friction coefficient

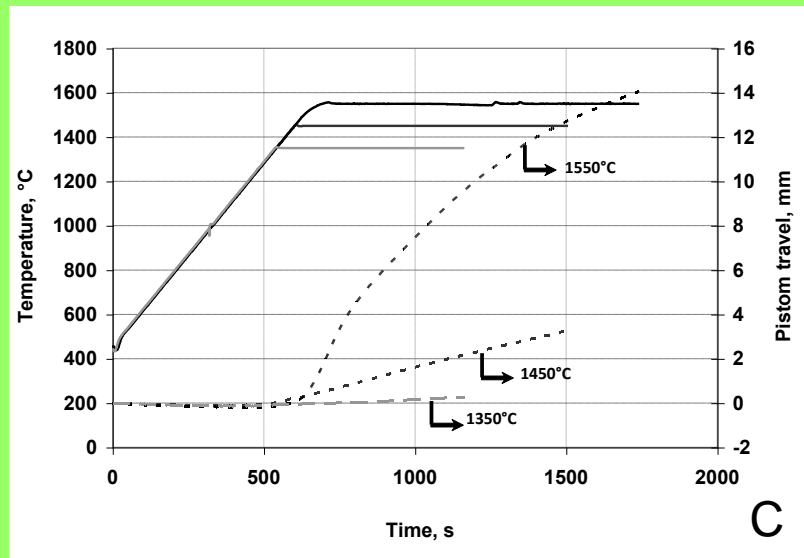
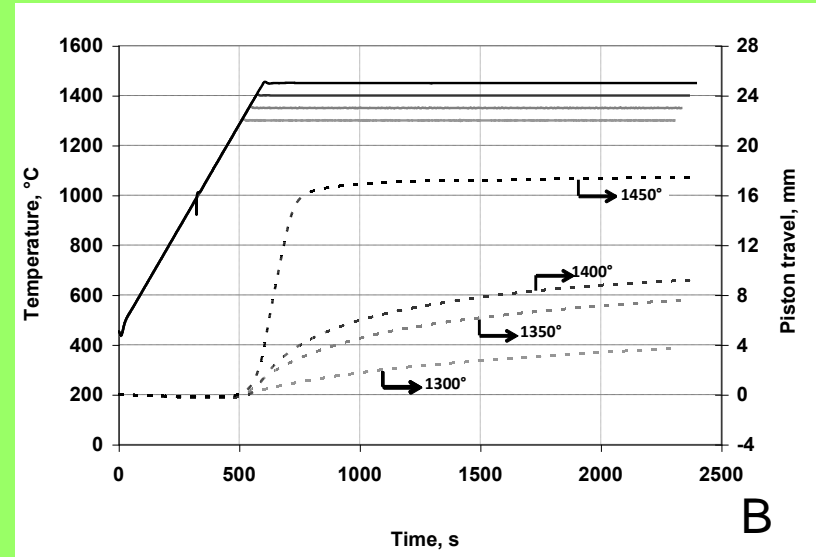
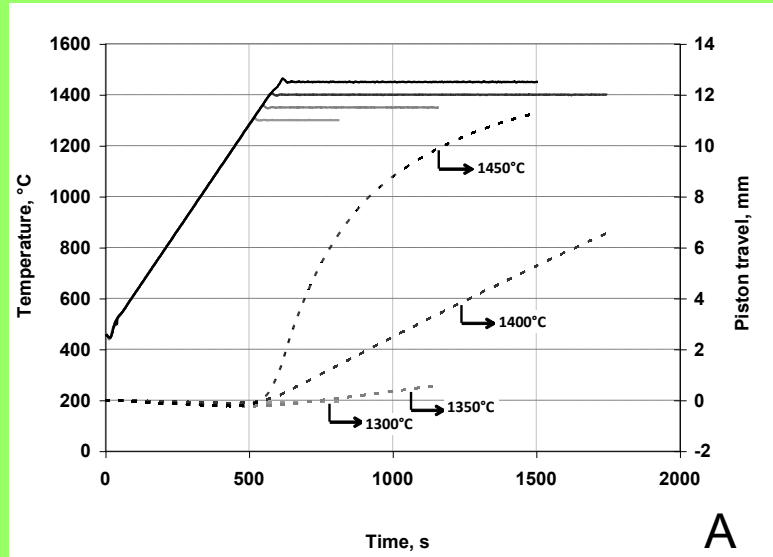


$$f_{av} = \frac{E_{fr}}{2 \cdot F_{fr} \cdot D}$$

ZrO₂ bal: 10 mm; Load: 1 and 2 N;
Displacement: 1000 μm; Frequency: 1 Hz

E_{fr} – friction work; F_{fr} – friction force; D - displacement

Kinetics of plastic deformation

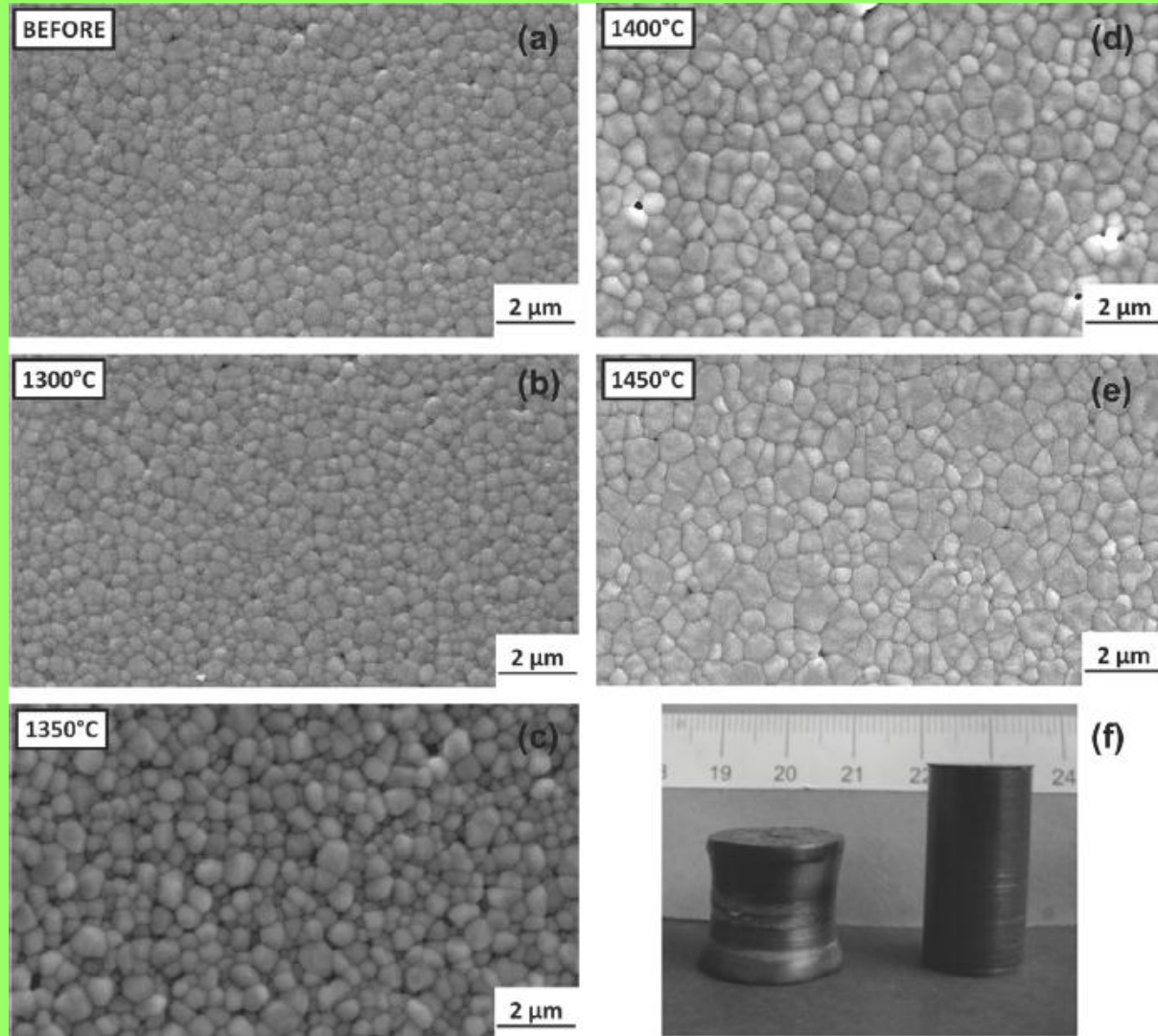


A: 3Y-ZrO₂

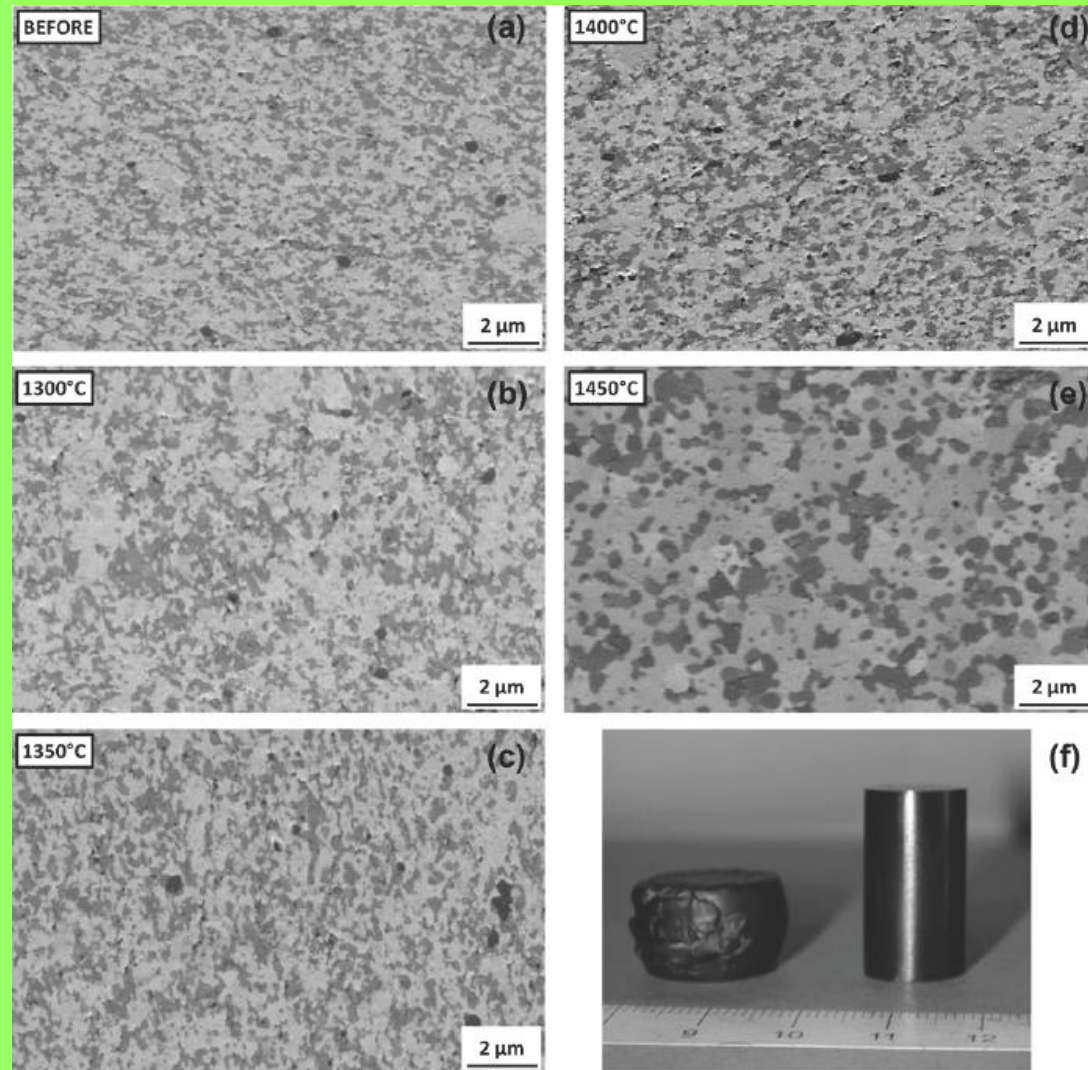
B: ZrO₂-TiCN 60/40 without disc

C: ZrO₂-TiCN 60/40 with disc

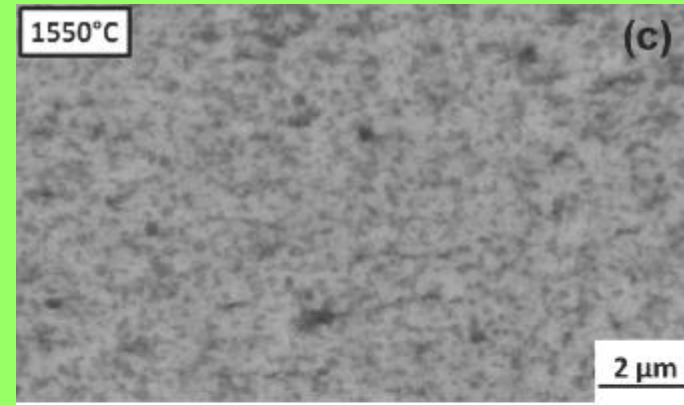
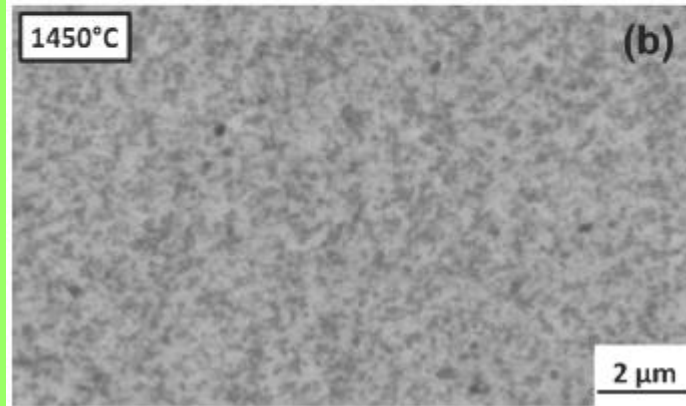
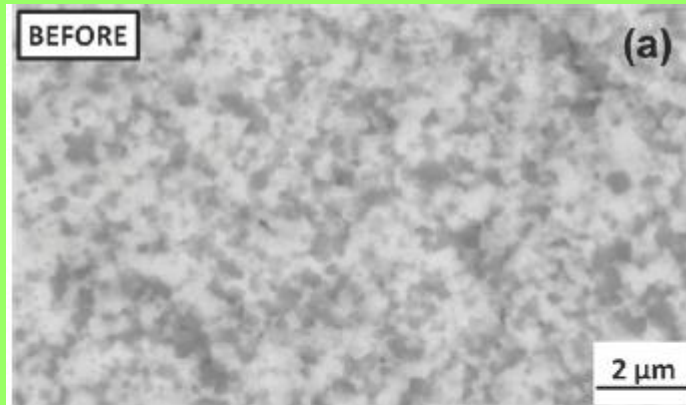
Microstructure and shape of 3Y-ZrO₂ samples before and after deformation



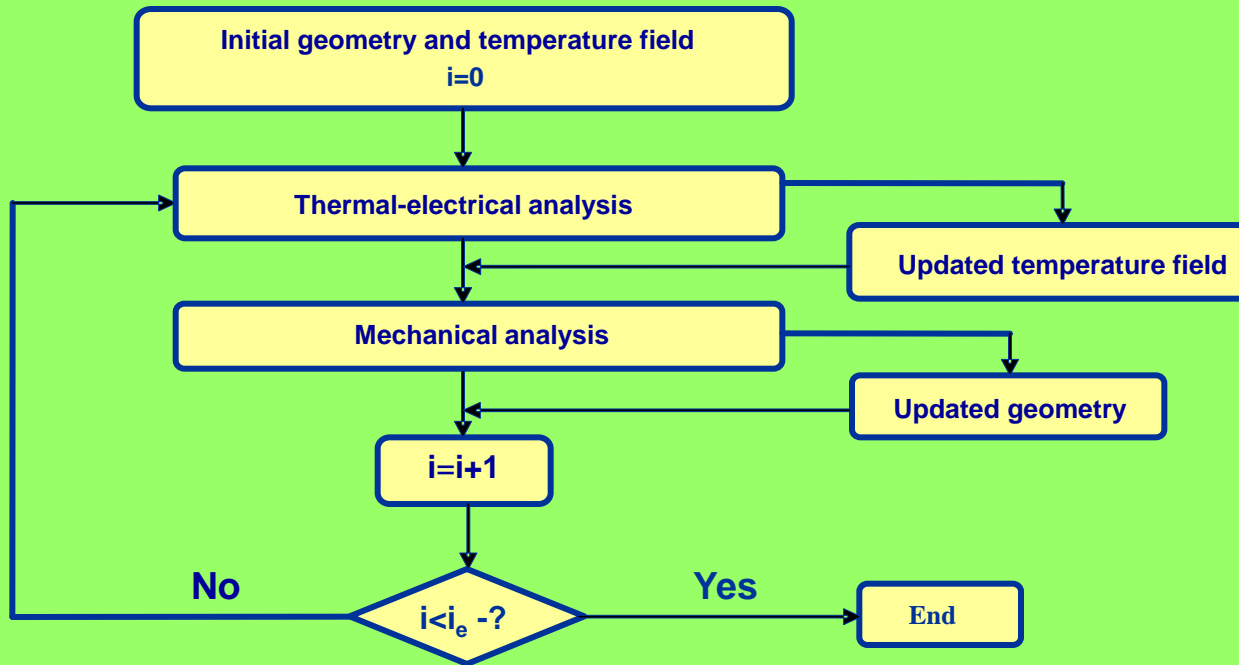
Microstructure and shape of ZrO_2 -TiCN samples after deformation without SiC discs



Microstructure and shape of $\text{ZrO}_2\text{-TiCN}$ samples after deformation with SiC discs

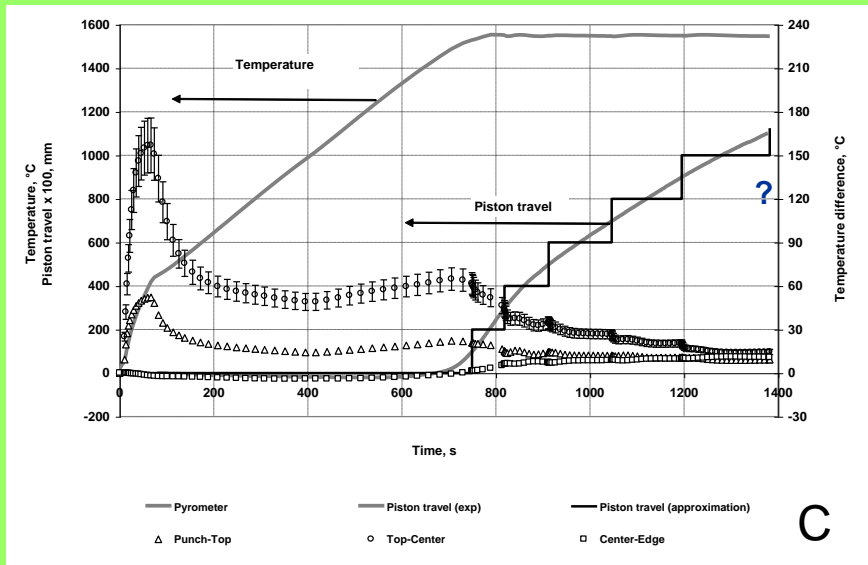
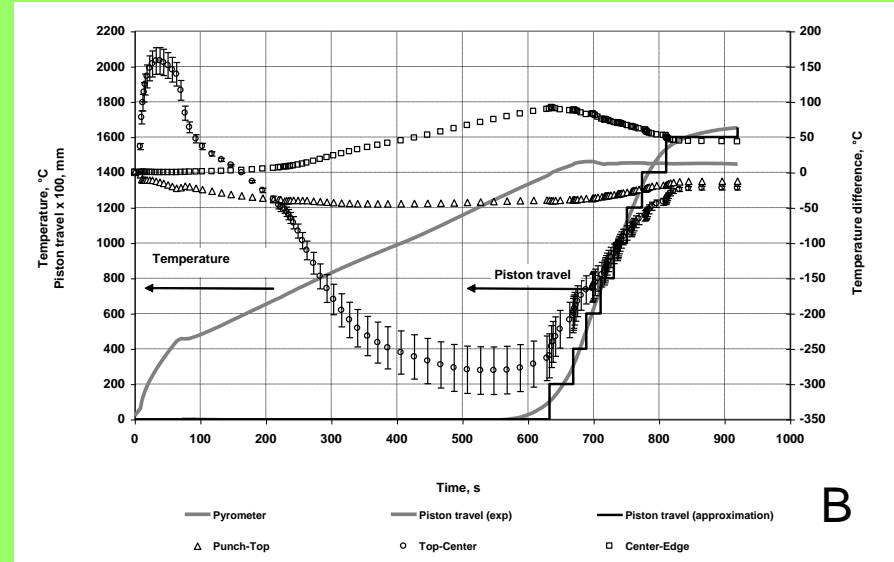
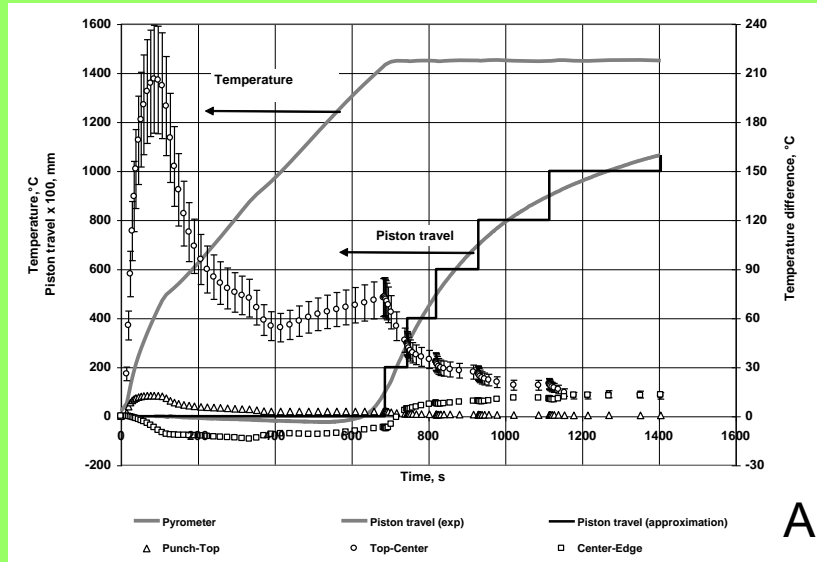


Iteration procedure of FEM analysis



$$\dot{\epsilon}_{eff} = A_0 \frac{\sigma_{eff}^n}{d^p} \exp\left(-\frac{Q}{RT}\right)$$

Results of FEM modeling

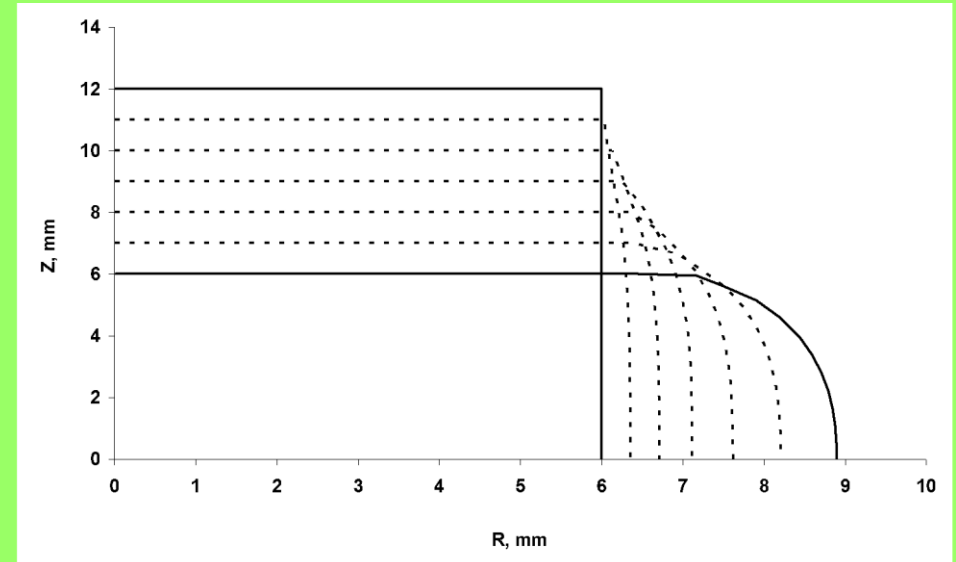
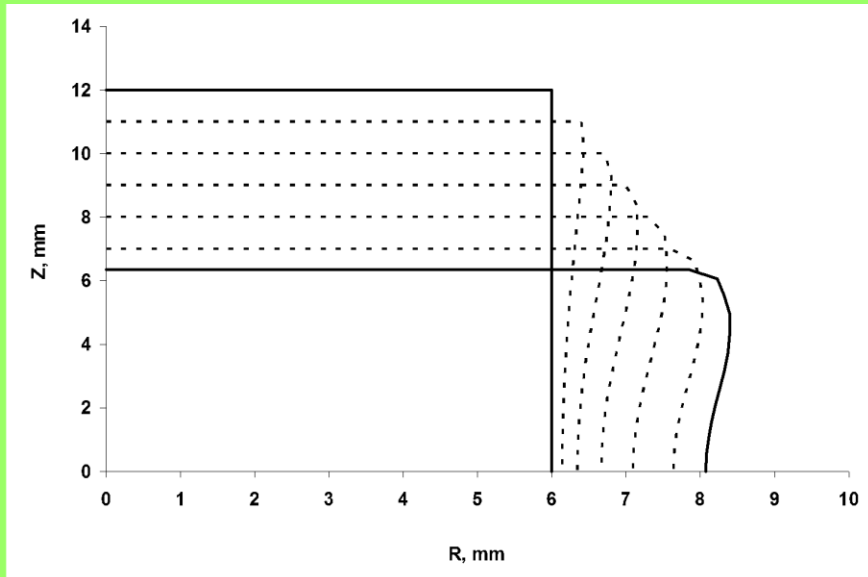


A: 3Y-ZrO₂

B: ZrO₂-TiCN 60/40 without disc

C: ZrO₂-TiCN 60/40 with disc

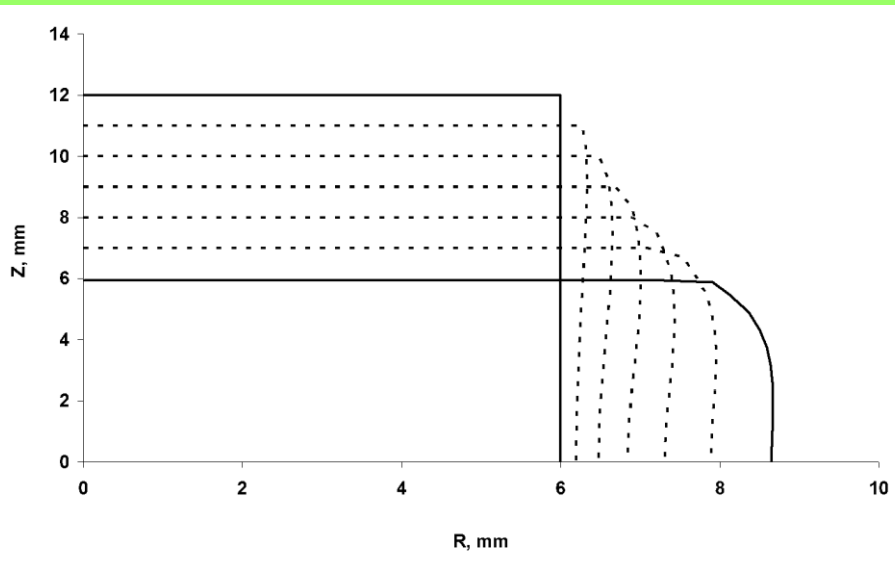
Results of FEM modeling



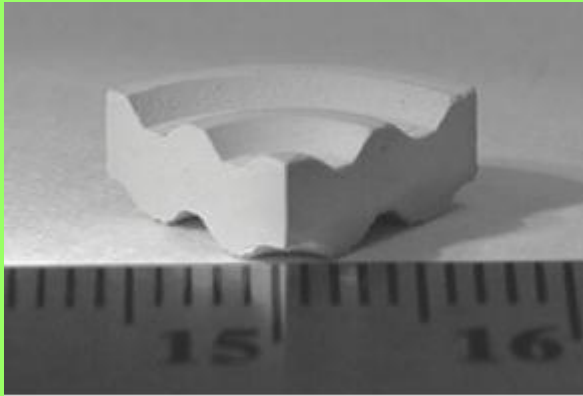
A: 3Y-ZrO₂

B: ZrO₂-TiCN 60/40 without disc

C: ZrO₂-TiCN 60/40 with disc



Examples of ceramics forming in SPS apparatus



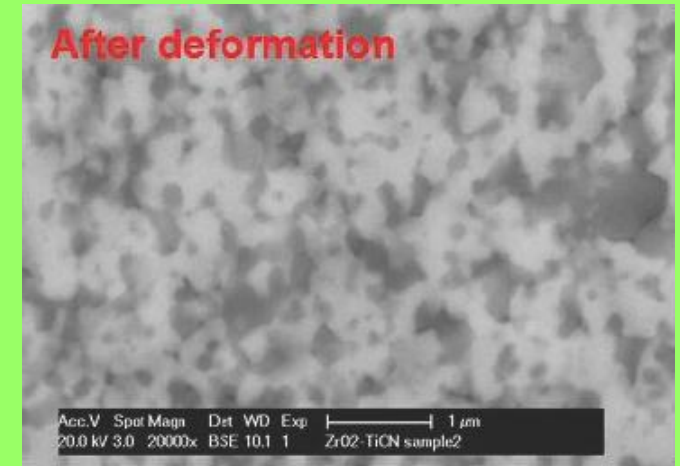
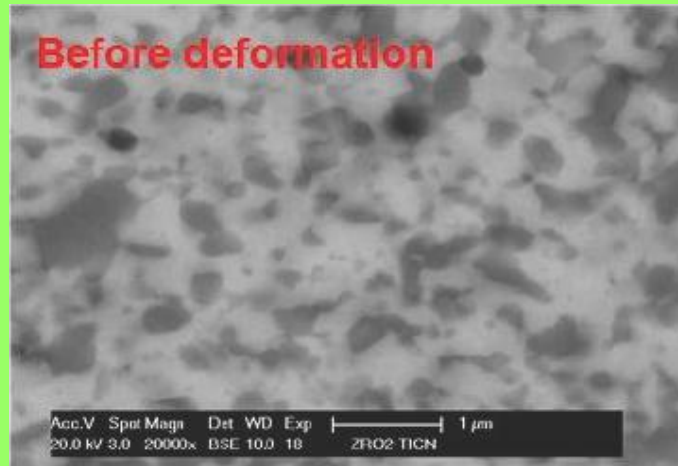
$\text{Al}_2\text{O}_3\text{-ZrO}_2\text{-MgAl}_2\text{O}_4$



Jiang D., Hulbert D.M., Kuntz J.D., Anselmi-Tamburini U., Mukherjee A.K. Materials Science and Engineering A 463 (2007) 89–93



$\text{ZrO}_2\text{-TiCN}$



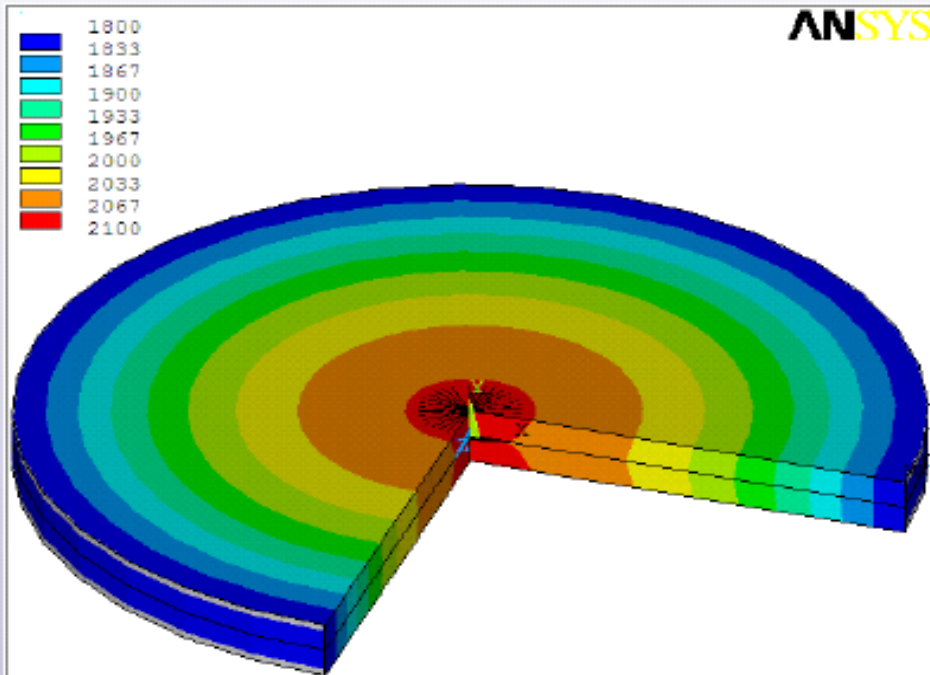
Main conclusions (section # 3)

- SPS technique can be successfully applied for plastic deformation of both conductive and non-conductive ceramics at deformation rates in the range of 10^{-2} - 10^{-3} s⁻¹.
- The presence of secondary TiCN phase retards the grain growth of Zirconia.
- Predominant electrical current paths can essentially influence the temperature distribution in a sample and its shape after deformation. The current paths can be controlled by die design.
- Temperature gradient is especially large at heating and at the beginning of deformation. The gradient diminishes with decrease in sample height and during dwell period at maximal temperature.
- An innovative subsequently coupled thermal–electrical–mechanical FEM procedure was developed to predict temperature, current, voltage as well as stress distributions and geometrical sample change during deformation in a SPS apparatus.

Optimization of die design

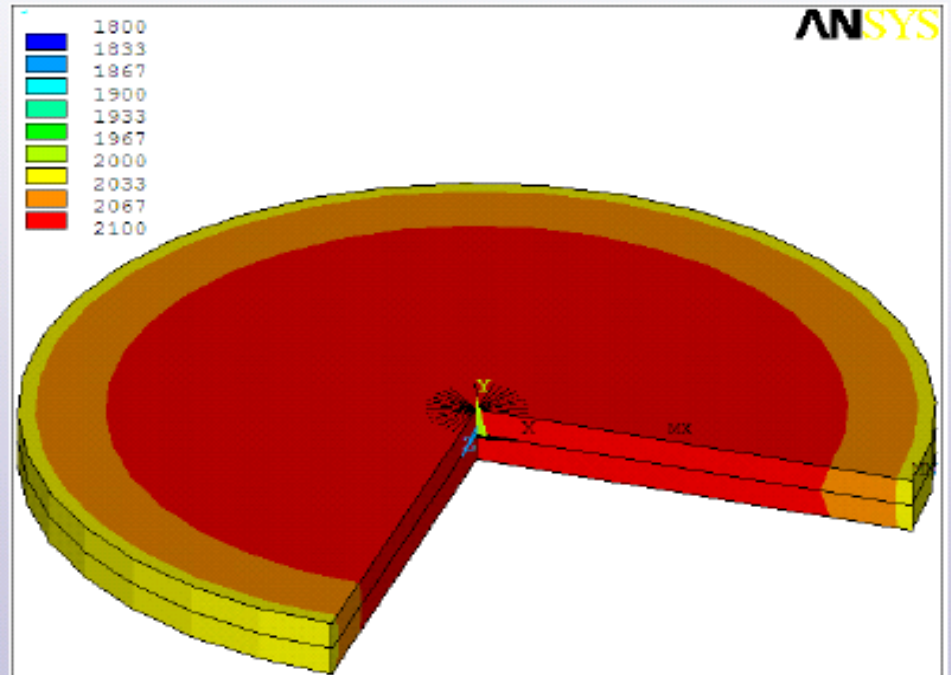
**Temperature Distribution in Sample;
Mold dia. 200 mm, 2100°C, 100 K/min**

200 Ø 1. Experiment



$\Delta T > 250K$

200 Ø Mold optimized

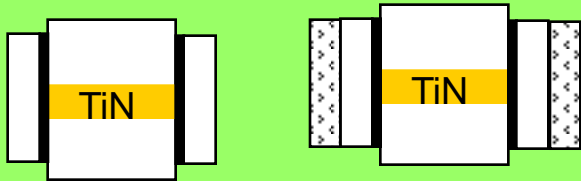


$\Delta T < 50K$

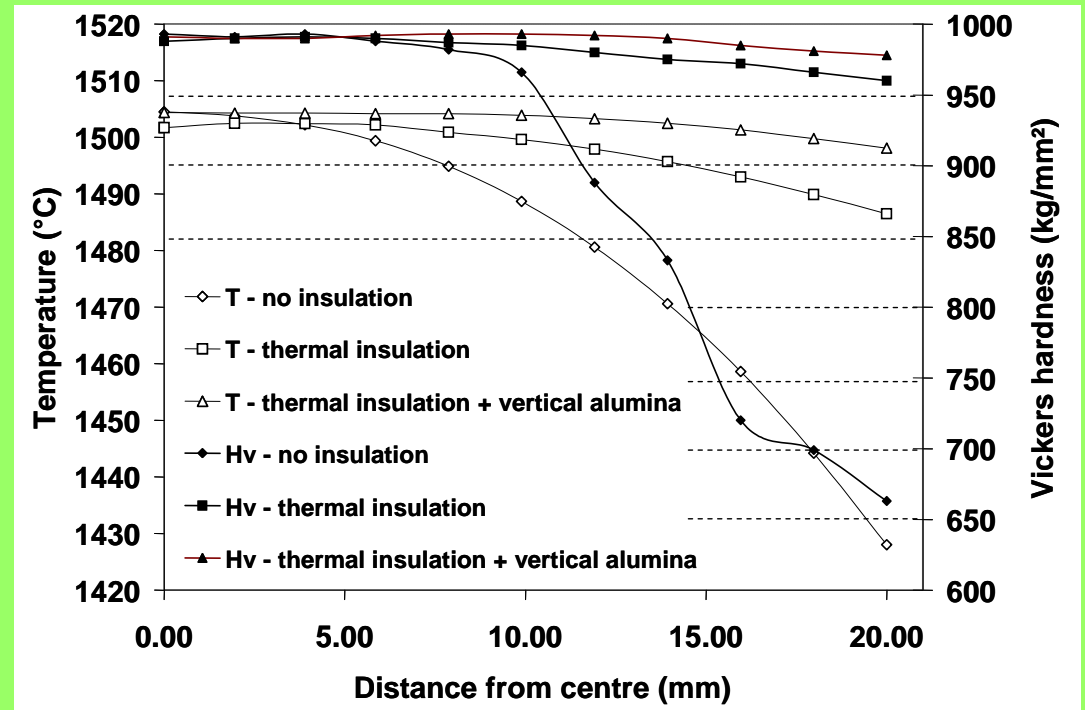
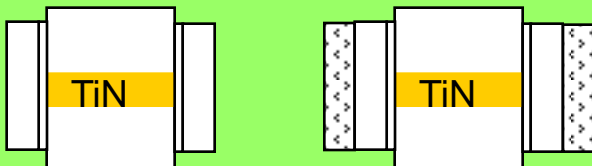
Courtesy: FCT systeme

Influence of insulation on temperature and hardness distribution

A. 40 mm diameter die
vertical **graphite** paper



B. 40 mm diameter die
vertical **alumina** paper



Further work

- **The change from explanation to prediction of observed at SPS phenomena is necessary.**
- **The development of a simple method for determination of rheological characteristics of materials needed for SPS modeling is desirable.**
- **The creation of properties data base for materials processed by SPS technology and for materials used for tool is advisable.**
- **The special subroutines for modeling of SPS processes taking into account a complex rheology of sintered materials should be written.**

Acknowledgment

A. Laptev thanks Research Council of Katholieke Universiteit Leuven for giving possibility of Spark Plasma Sintering investigation in Department of Metallurgy and Materials Engineering by fellowship F/02/096 and Ministry of Education and Science of Ukraine for financial support of research through project No 0107U001301

A tall, cylindrical white lighthouse with a red lantern room and a red gallery, situated on a concrete base in the ocean. The base has several windows and blue pipes. A smaller white structure is visible on a pier to the right. The sky is clear blue, and the water is dark blue with small waves. The text "Thank You for attention !!!" is overlaid in blue on the right side of the image.

Thank You for attention !!!